

2000

## LECTURE #2

## BREAKDOWN OF GROWTH

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UCLA

- 2-Deflator Method

$$\Delta Y^* = w^* \Delta L^* + (\rho + \delta) \Delta K^* + R^*$$

- Traditional TFP Method

$$\Delta Y = \phi_L \Delta L + \phi_K \Delta K + R$$

$$Y^* \neq Y \quad L^* \neq L \quad K^* \neq K$$

but  $s_L = \frac{w^* L^*}{Y^*} = \frac{\phi_L L}{Y}$

$$s_K = \frac{(\rho + \delta) K^*}{Y^*} = \frac{\phi_K K}{Y}$$

- So both methods look similar in the following form:

$$\frac{R^*}{Y^*} = \frac{\Delta Y^*}{Y^*} - s_L \frac{\Delta L^*}{L^*} - s_K \frac{\Delta K^*}{K^*}$$

and

$$\frac{R}{Y} = \frac{\Delta Y}{Y} - s_L \frac{\Delta L}{L} - s_K \frac{\Delta K}{K}$$

- But they are different

$$Y^* = \frac{\text{Value Added}}{\text{GDP Deflator}}$$

$K^*$  = Capital measured in GDP Baskets

.....

$Y$  = Output in yards of cloth or value added at constant prices

$K$  = Capital measured as number of machines or as an index of capital goods at constant prices

- 2-Deflator Method does not require us to have data on relative prices of output or on relative price of inputs.

- This is very important because
  - a) We hardly ever have prices at the firm level.
  - b) We often do not have them at the industry level.
  - c) When we have them, they are very often unreliable.
- Also, 2-Deflator Method is very easy to apply, hence very attractive.
- But does it work??

We will show that it does work.

- 2 Variations:

a) Do basic calculations using the 2-Deflator Method, then adjust for price changes.

b) Use 2-Deflator Method without price adjustments.

- Price adjustment is simple.

$$\frac{\Delta Y^*}{Y^*} = \frac{\Delta Y}{Y} + \frac{\Delta P}{P}$$

so

$$\frac{\Delta Y^*}{Y^*} - \frac{\Delta P}{P} = s_L \frac{\Delta L^*}{L^*} + s_K \frac{\Delta K^*}{K^*} + \left[ \frac{R^*}{Y^*} - \frac{\Delta P}{P} \right]$$

$$\frac{\Delta Y}{Y} = s_L \frac{\Delta L^*}{L^*} + s_K \frac{\Delta K^*}{K^*} + \frac{R^{**}}{Y^*}$$

where

$$\frac{R^{**}}{Y^*} = \left[ \frac{R^*}{Y^*} - \frac{\Delta P}{P} \right]$$

- Biggest Point:

2-Deflator Method multiplies by a huge factor (probably between 10 and 100) the range of data that we can study via breakdown of growth.

- One cannot exaggerate the importance of this point.

- As we did yesterday, we compare the 2-Deflator with the Jorgenson Method, comparing both 1-year changes and changes over 5-year non-overlapping periods. We do this for the

$$\text{Labor Contribution: } s_L \frac{\Delta L}{L} \quad \text{with} \quad s_L \frac{\Delta L^*}{L^*}$$

$$\text{Capital Contribution: } s_K \frac{\Delta K}{K} \quad \text{with} \quad s_K \frac{\Delta K^*}{K^*}$$

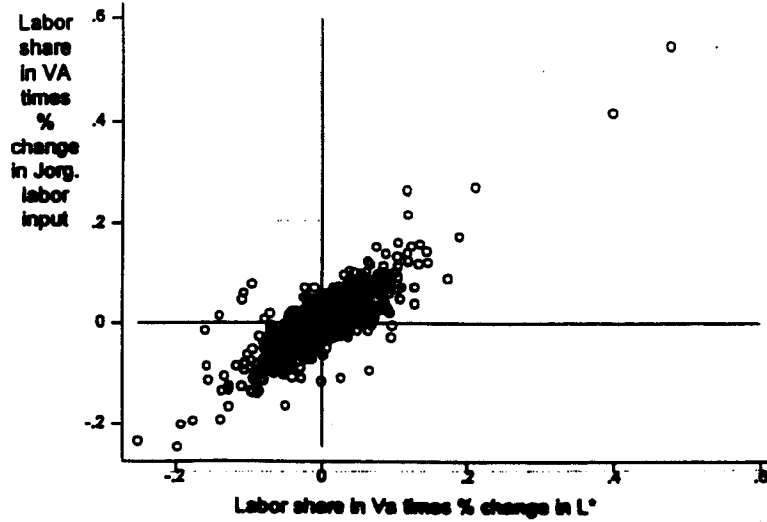
$$\text{Calculated TFP: } R \quad \text{with} \quad R^*$$

Value Added under

$$\text{both concepts: } \frac{\Delta Y}{Y} \quad \text{with} \quad \frac{\Delta Y^*}{Y^*}$$

(Latter shifts Jorgenson quantity variable to a value added basis.)

Figure 1  
Jorgenson vs Two-Deflator Labor Contribution  
Yearly Data 1948-91  
( $r=.8095$ )



5-Year Data (Annual Average Rates)  
( $r=.8359$ )



DATA from JORGENSEN KLEM3J

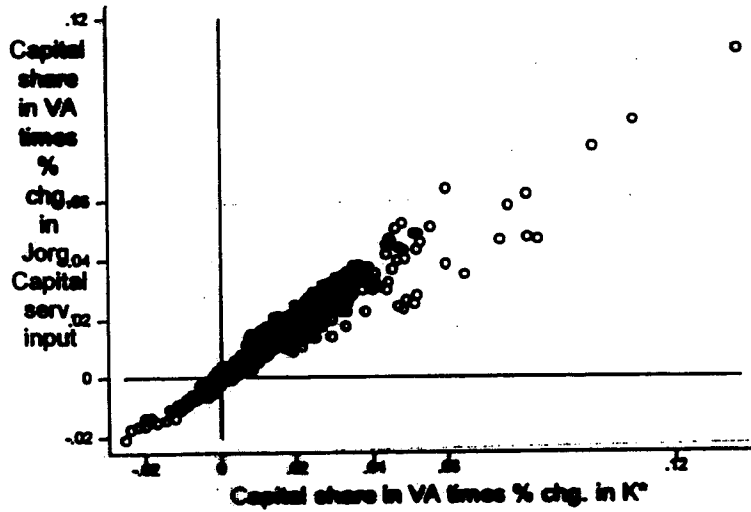
3.5 Sector Breakdown

(minus petroleum & govt enterprises)

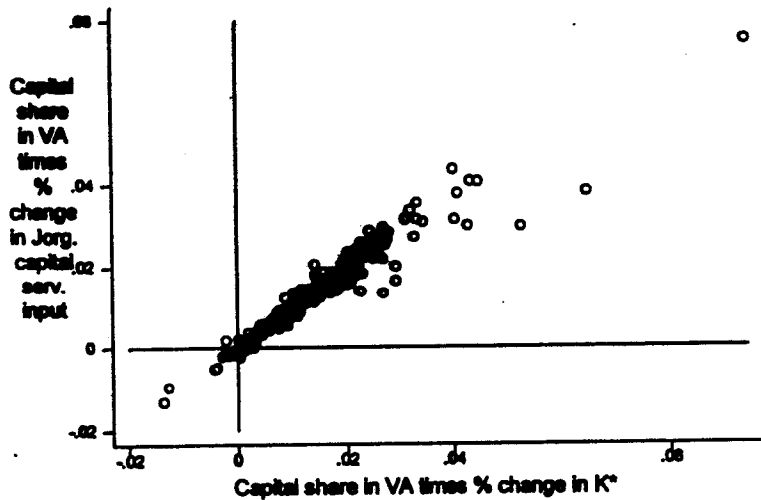


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Figure 2  
Jorgenson vs Two-Deflator Capital Contribution  
(Yearly Data) 1948-51  
( $r=.9647$ )



5-Year Data (Annual Average Rates)  
( $r=.9634$ )



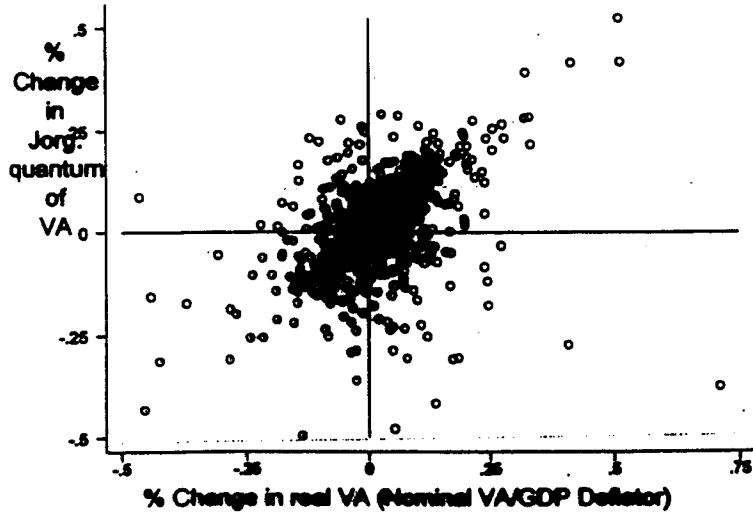
DATA from JORGENSEN KLEM 3.5

3.5 Sector Breakdown

(minus petroleum and gov enterprise)

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Figure 3  
Average Rates of Growth of the Quantity of Value Added  
Jorgenson vs Two-Deflator Methods  
(Yearly Data)  
( $r=.4733$ )



5-Year Data (Annual Average Rates)  
( $r=.5245$ )

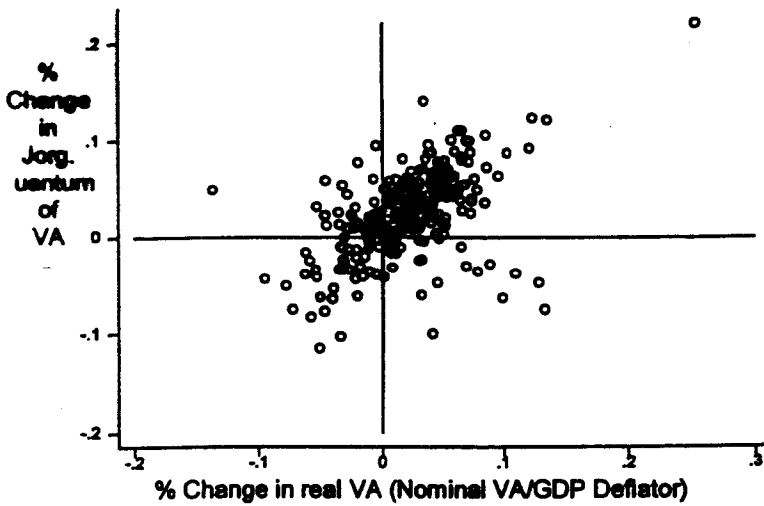
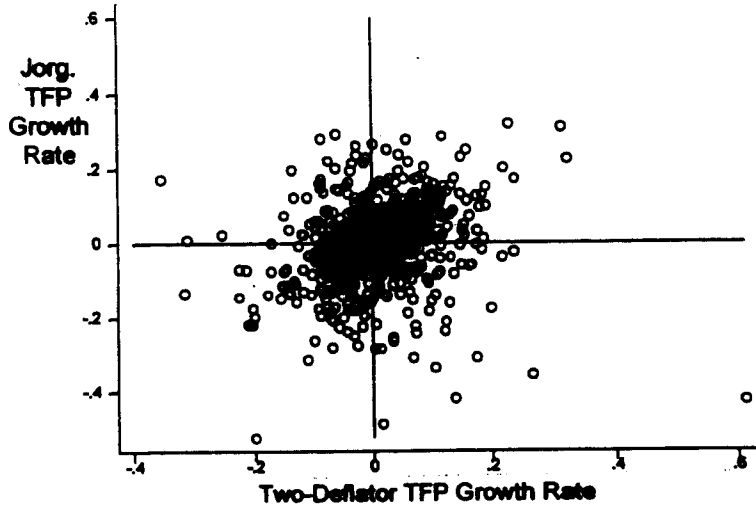
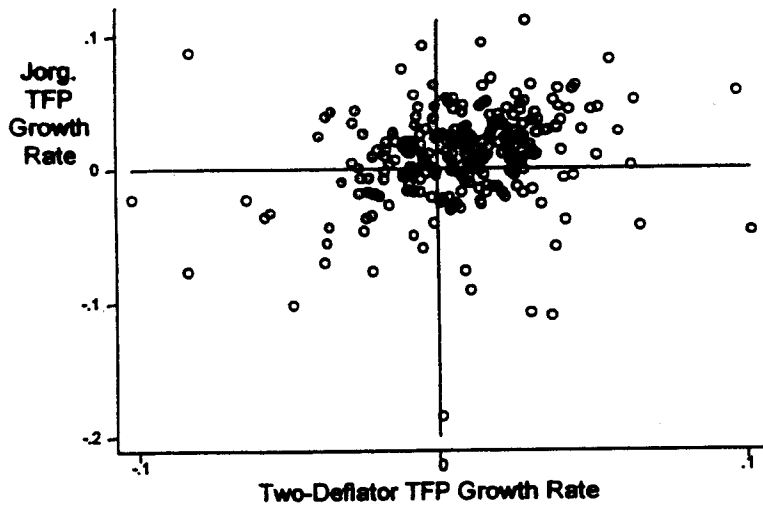


Figure 4  
Jorgenson vs Two-Deflator TFP Growth  
Yearly Data  
( $r=.2353$ )



5-Year Data (Annual Average Rates)  
( $r=.2391$ )

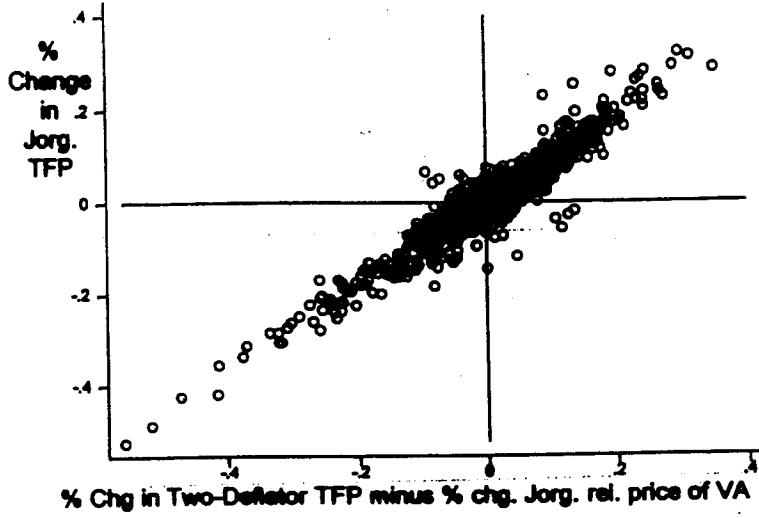


- Now, we look at the effects of doing price adjustments:

a) Shift 2-Deflator  $\Delta TFP$  to a “Jorgenson Basis” by subtracting  $\Delta P_{va}/P_{va}$ .

b) Shift “Jorgenson”  $\Delta TFP$  to a “2-Deflator Basis” by adding  $\Delta P_{va}/P_{va}$ .

Figure 5  
Jorgenson vs "Two-Deflator Adjusted" TFP Growth  
Yearly Data  
( $r=.9385$ )



5-Year Data (Annual Average Rates)  
( $r=.9418$ )

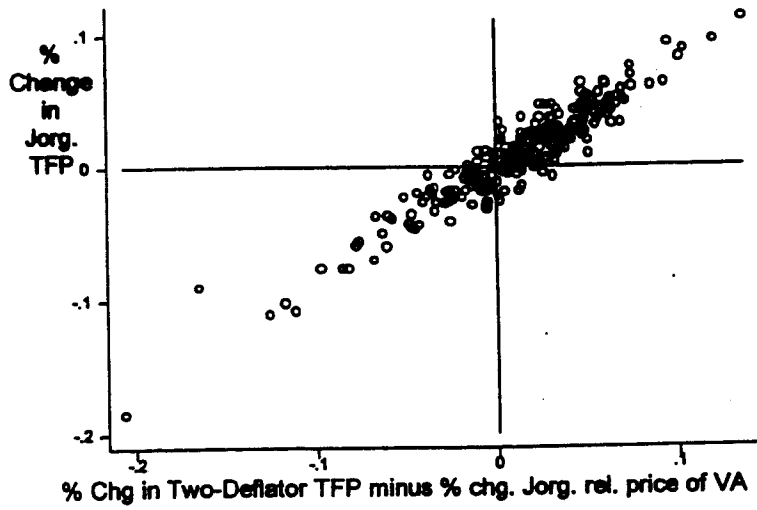
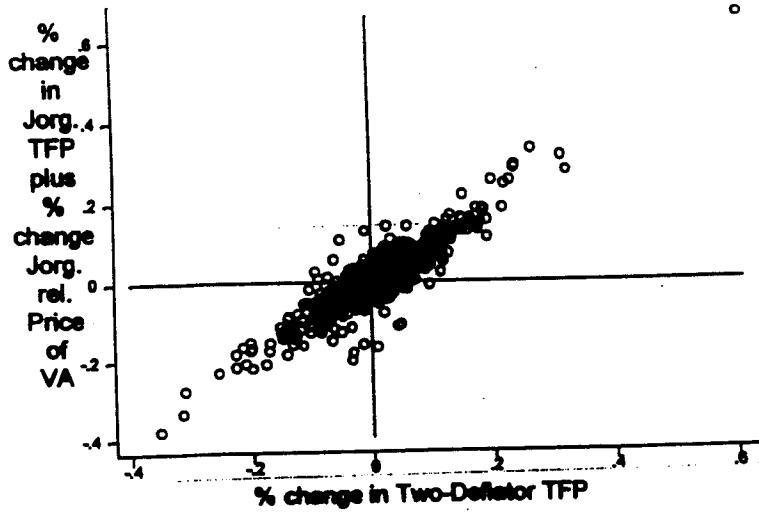
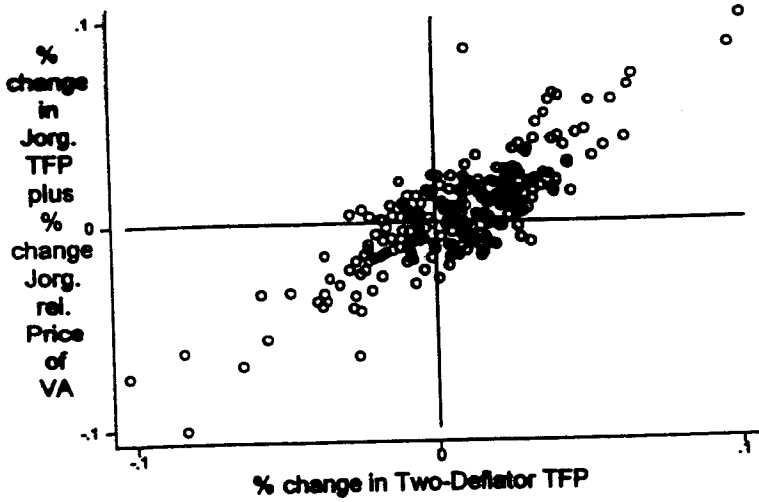


Figure 6  
"Jorgenson Modified" vs Two-Deflator TFP Growth  
Yearly Data  
( $r=.8827$ )

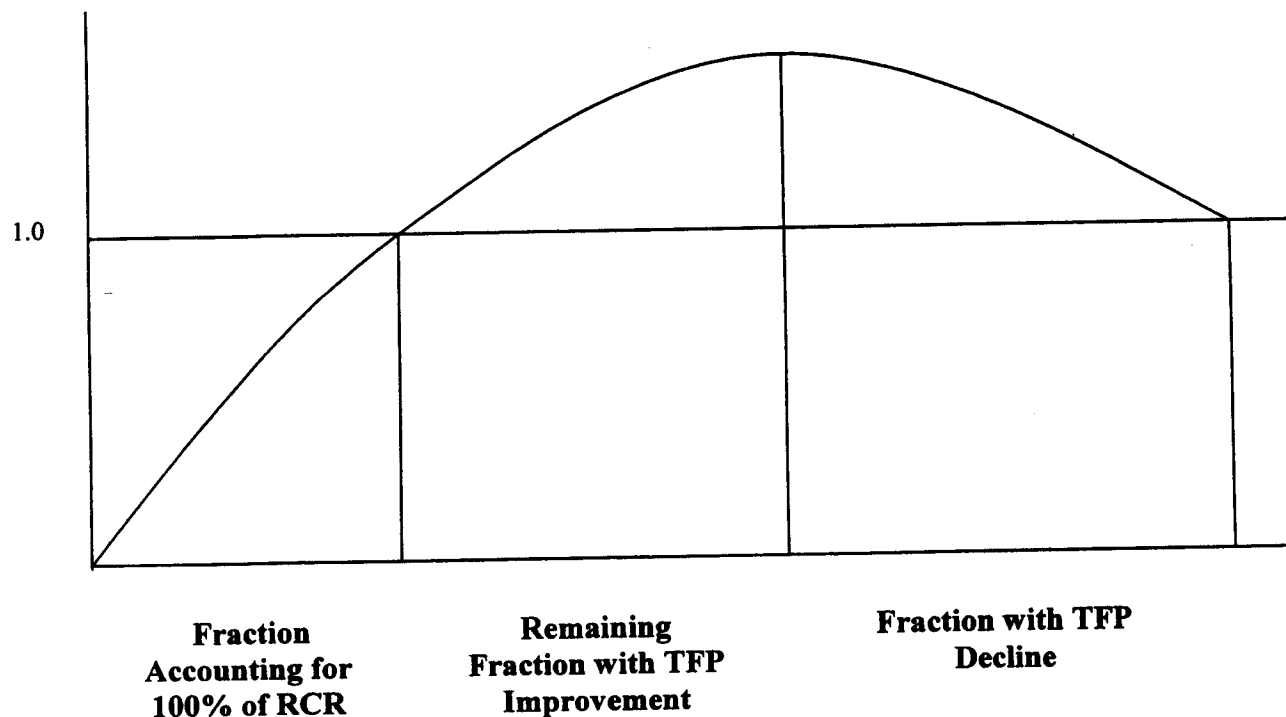


5-Year Data (Annual Average Rates)  
 $r=.8317$



- Now, we try to extract inferences from the data.
- My Presidential Address gave a lot of attention to instances of negative changes in TFP – i.e. of increasing real costs.

## SUNRISE-SUNSET DIAGRAM



- The three indicated fractions nicely summarize the “shape” of a Sunrise-Sunset Diagram.
- To give an idea of the rates of TFP growth involved, we have the second panel on each page.
- This presents overall rates of TFP growth within each of the cells defined in the first breakdown.
- I call attention to the top comparison in each panel.-

Why? Because this uses the 2-Deflator results without any price adjustments.



- Please note how close the results are in all three comparisons within each panel. But especially the top panel. The pictures emerging from Jorgenson and the unadjusted 2-Deflator calculations are virtually identical.

TABLE 11  
Distribution of Initial Value Added by TFP Performance  
Yearly Changes (1419 Observations, 1948-1991)

	Fraction Accounting for 100 % of RCR A	Remaining fraction with TFP improvement B	Fraction with TFP decline C	All
Jorgenson	0.041	0.550	0.409	1.000
2DFL	0.044	0.529	0.427	1.000
Jorgenson	0.041	0.550	0.409	1.000
2DFLadj.	0.068	0.536	0.396	1.000
2DFL	0.044	0.529	0.427	1.000
Jorg. modified	0.015	0.518	0.467	1.000

Average annual Rate of TFP Improvements in Category

	Fraction Accounting for 100 % of RCR	Remaining fraction with TFP improvement	Fraction with TFP decline	All
Jorgenson	0.1952	0.0429	-0.0578	0.0080
2DFL	0.1634	0.0350	-0.0433	0.0073
Jorgenson	0.1952	0.0429	-0.0578	0.0080
2DFLadj.	0.1723	0.0467	-0.0633	0.0117
2DFL	0.1634	0.0350	-0.0433	0.0073
Jorg. modified	0.2321	0.0350	-0.0388	0.0036

Source: Calculations of year-to-year changes in value added and in real cost reduction (% $\Delta$ TFP) underlying Table 8 (for Jorgenson and 2DFL), Column 2 of Table 9 (for 2DFLadj) and for column 1 of Table 10 (for Jorg. modified).

TABLE 12  
Distribution of Initial Value Added by TFP Performance  
Average Annual Rates over Five-year Periods (264 Observations, 1948-1988)

	Fraction Accounting for 100 % of RCR	Remaining fraction with TFP improvement	Fraction with TFP decline	All
	A	B	C	
Jorgenson	0.178	0.481	0.341	1.000
2DFL	0.208	0.455	0.337	1.000
Jorgenson	0.178	0.481	0.341	1.000
2DFLadj.v	0.208	0.485	0.307	1.000
2DFL	0.208	0.455	0.337	1.000
Jorg. modified	0.095	0.530	0.375	1.000

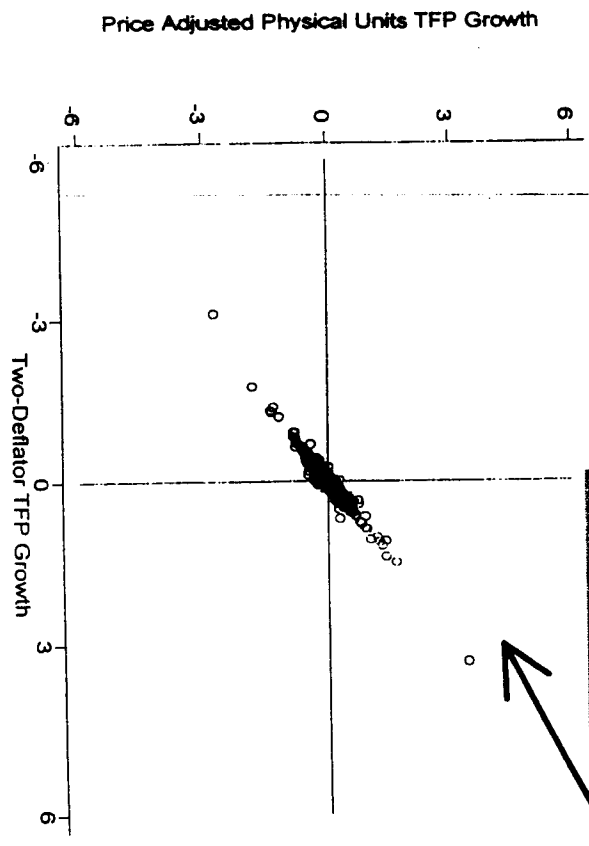
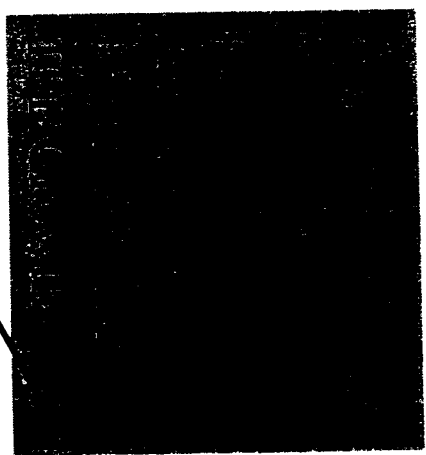
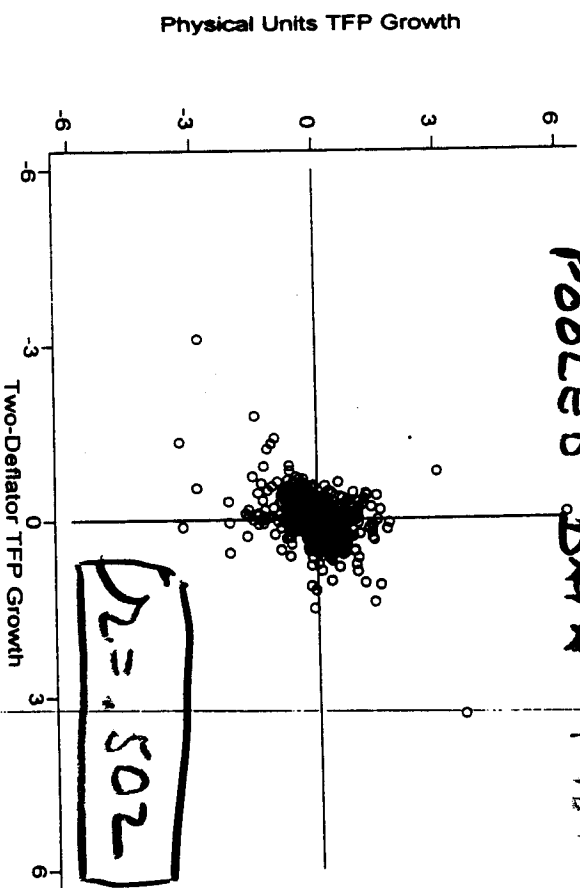
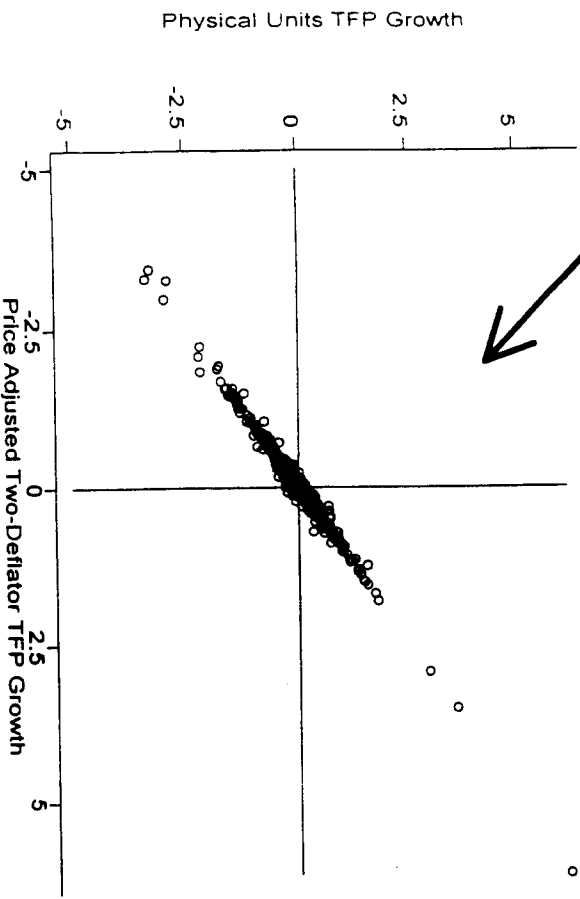
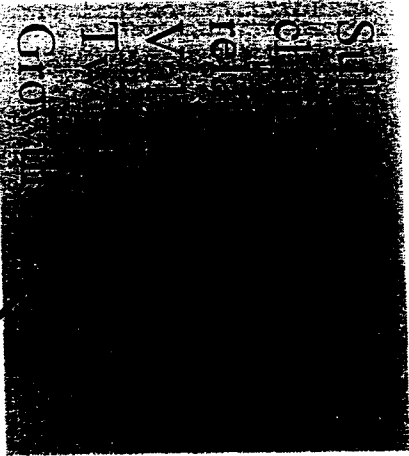
Average annual Rate of TFP Improvement in Category

	Fraction Accounting for 100 % of RCR	Remaining fraction with TFP improvement	Fraction with TFP decline	All
Jorgenson	0.0455	0.0188	-0.0266	0.0098
2DFL	0.0400	0.0137	-0.0185	0.0083
Jorgenson	0.0455	0.0188	-0.0266	0.0098
2DFLadj.	0.0629	0.0216	-0.0341	0.0131
2DFL	0.0400	0.0137	-0.0185	0.0083
Jorg. modified	0.0521	0.0123	-0.0173	0.0050

Source: Same as Table 11. Individual data points are five-year averages of the data points of Table 11.

- Now, we turn to a huge data set, NBER – 458 Manufacturing Industries, 1958-94.
- First, we look at the scatter of the 2-Deflator versus the Traditional  $\Delta$ TFP.
- As before, with price correction, they are almost the same.
- Without price correction, they look somewhat messy.

NER 458 MANUFACTURING SECTORS  
 Price Adjusting the TFP Growth Estimates  
 POOLED DATA 1950-1994



- But the correlation within each scatter are quite good even without price adjustment.
- They are way better when price adjustment is made.

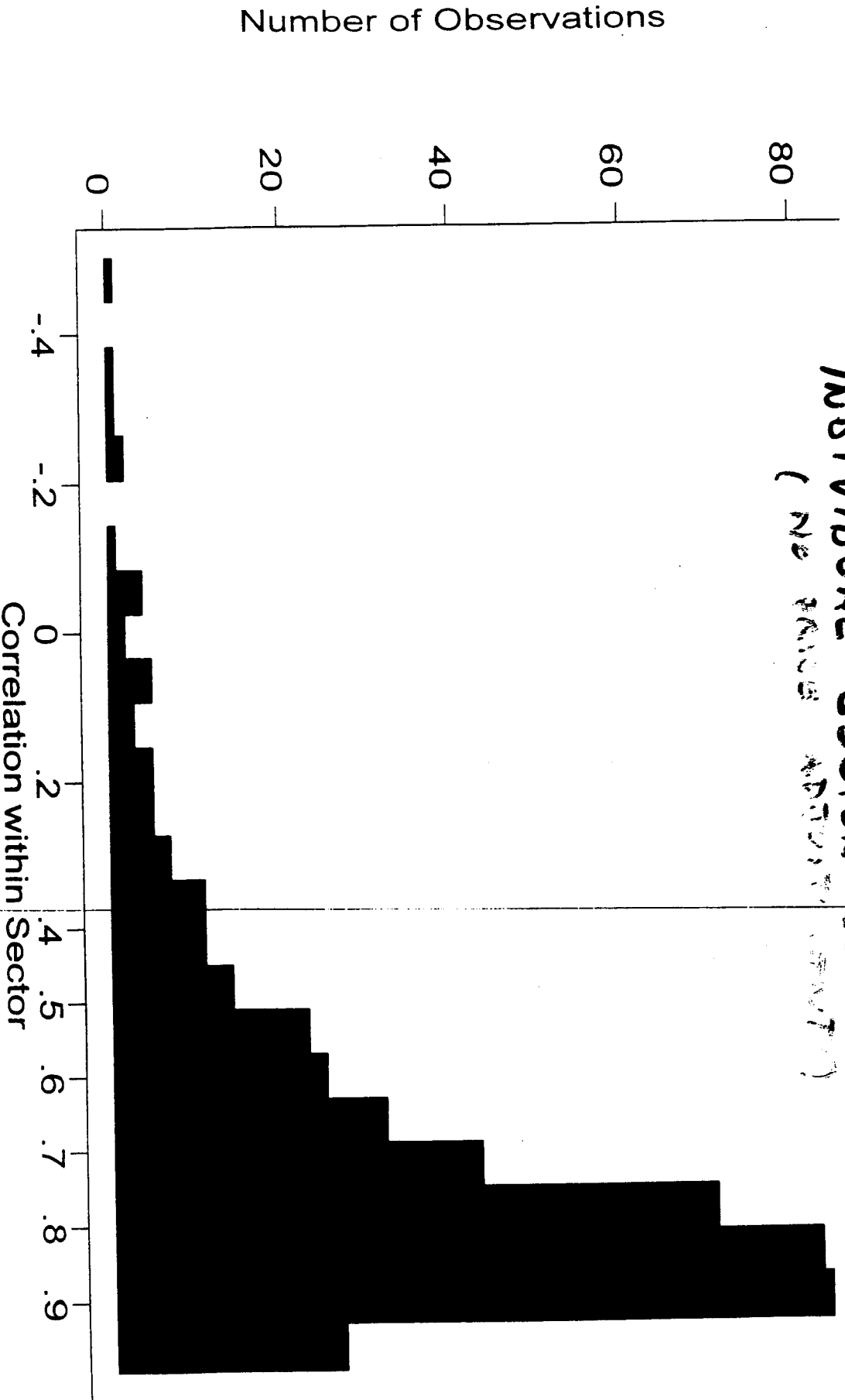
# Two-Deflator vs. Physical Units TFP Growth

458 (4-Digit SIC) Manufacturing Sectors, 1972-1994  
36 year-to-year changes each

INDIVIDUAL SECTOR

(No Panel Adjustment)

CORRELATIONS

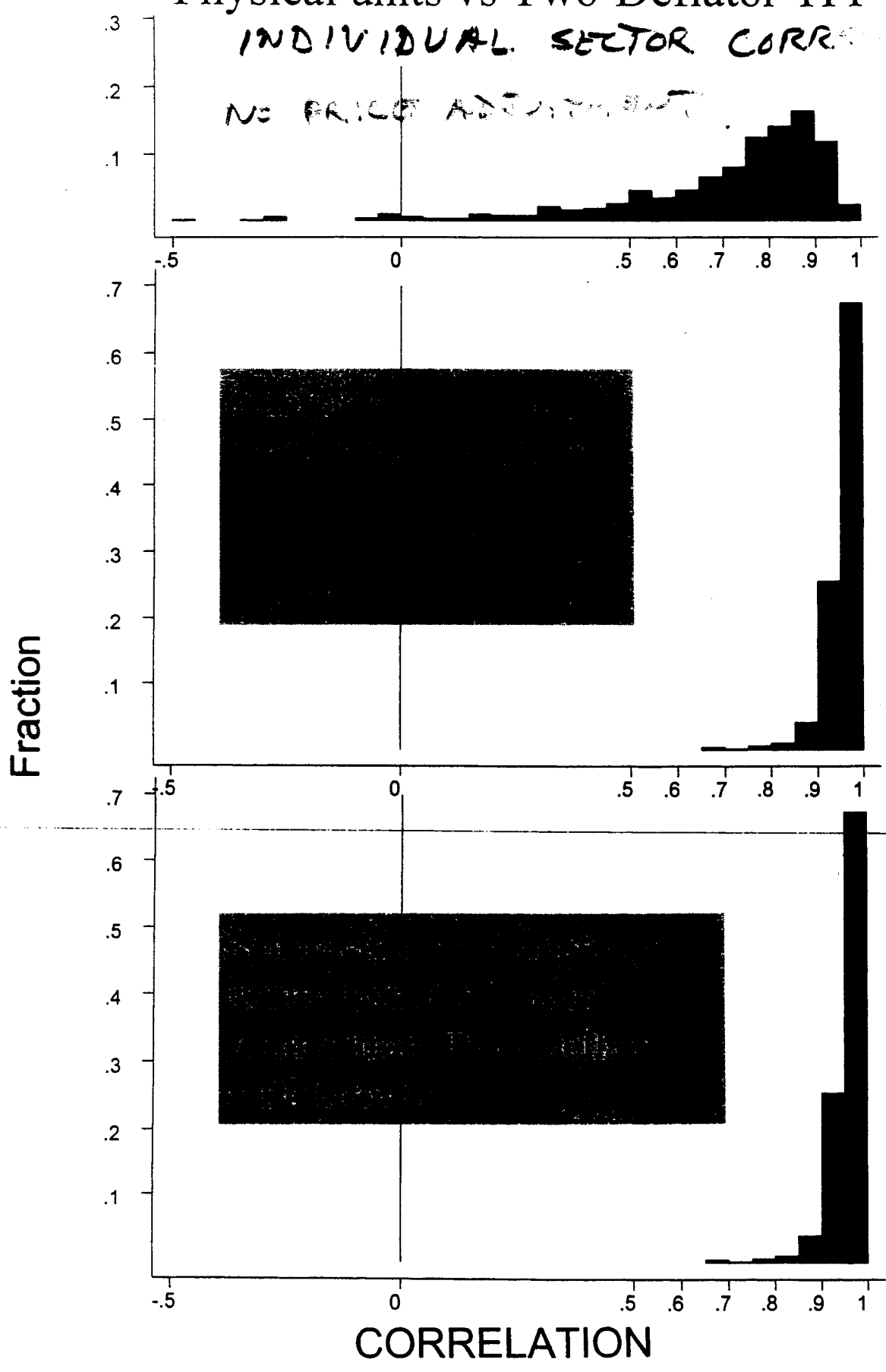


# Physical units vs Two-Deflator TFP

INDIVIDUAL SECTOR CORRELATION

25

NO PRICE ADJUSTMENT





- Now, we look at “predictions” using the NBER data. These all with 2-Deflator unadjusted data.
- Recall our “Growth Syndrome”:
  - First, we have real cost reductions ( $\Delta TFP > 0$ ).
  - This produces, in some order, investment and higher rates of return.
  - In the process, output goes up.
  - And maybe the employment of labor increases.

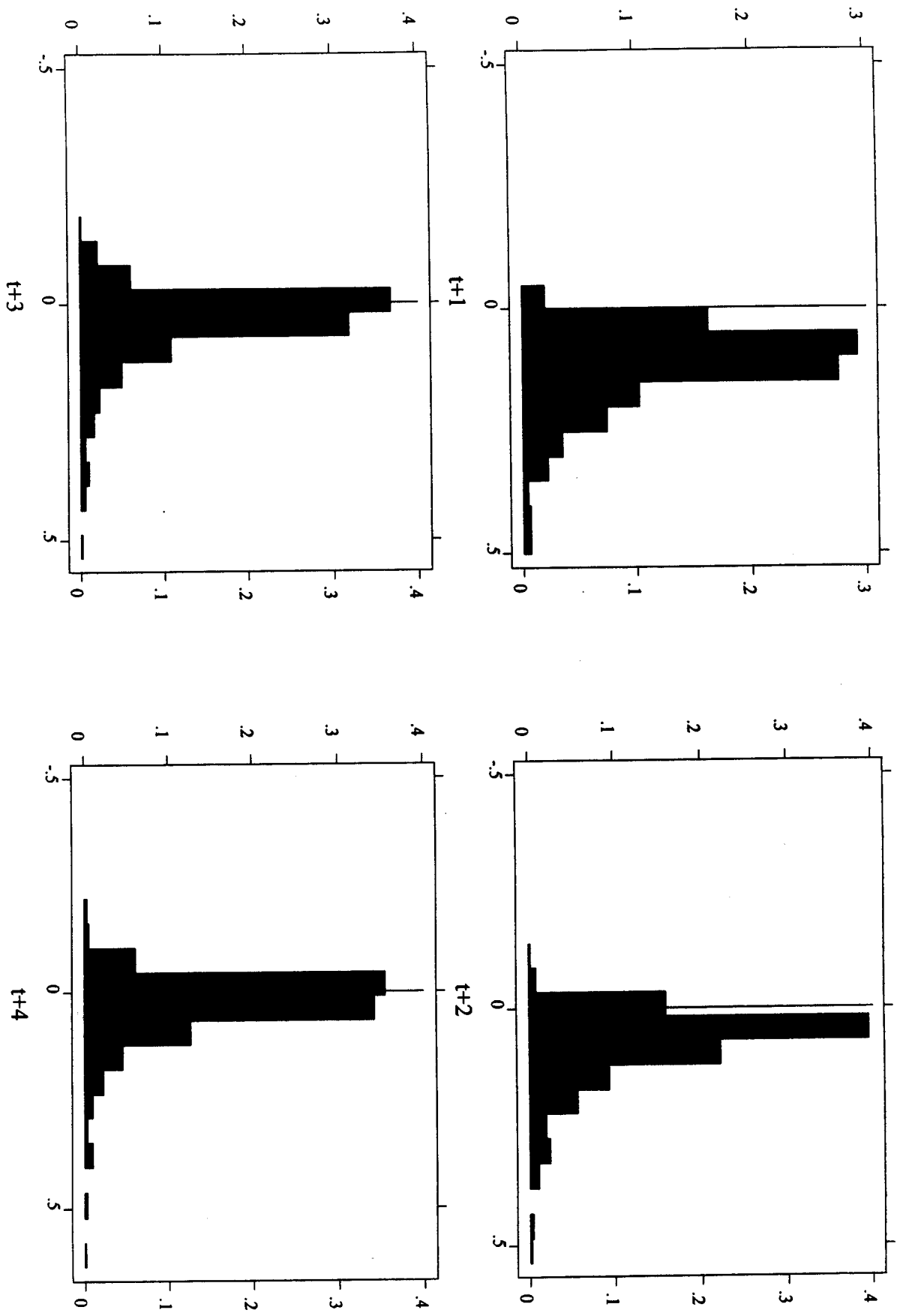
PREDICTING RATES OF RETURN

Variable	Obs	Mean	Std. Dev.	Min	Max
b <sub>1</sub>	458	0.118948	0.083929	-0.03946	0.501454
b <sub>2</sub>	458	0.082151	0.082294	-0.11355	0.537687
b <sub>3</sub>	458	0.041761	0.08405	-0.14202	0.537743
b <sub>4</sub>	458	0.036237	0.086746	-0.18346	0.633468

$$d\rho_j = \rho_{t+j} - \left[ \frac{\rho_{t-1} + \rho_t}{2} \right]$$

$$d\rho_j = a + \cancel{b_j} \Delta TFP_t + e$$

Data Source: NBER 458 Manufacturing Industries Database from 1958 to 1992



Distribution of Coefficient for Rate of Return

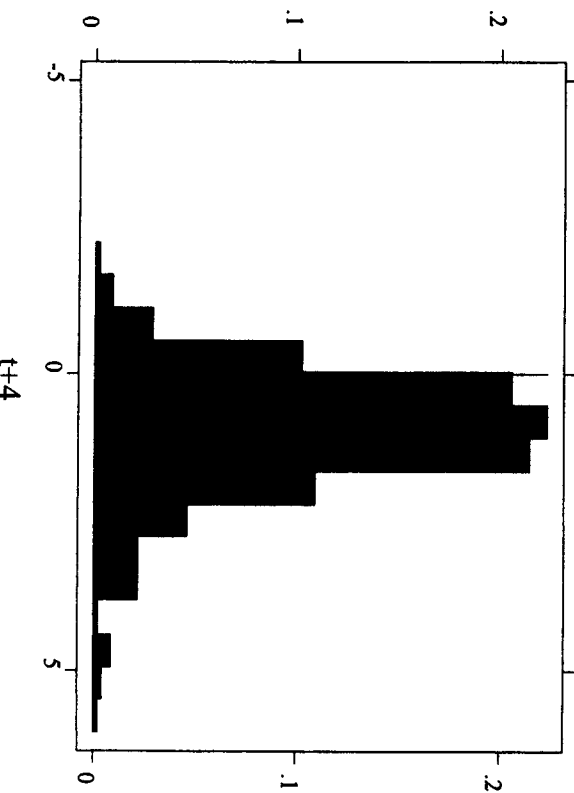
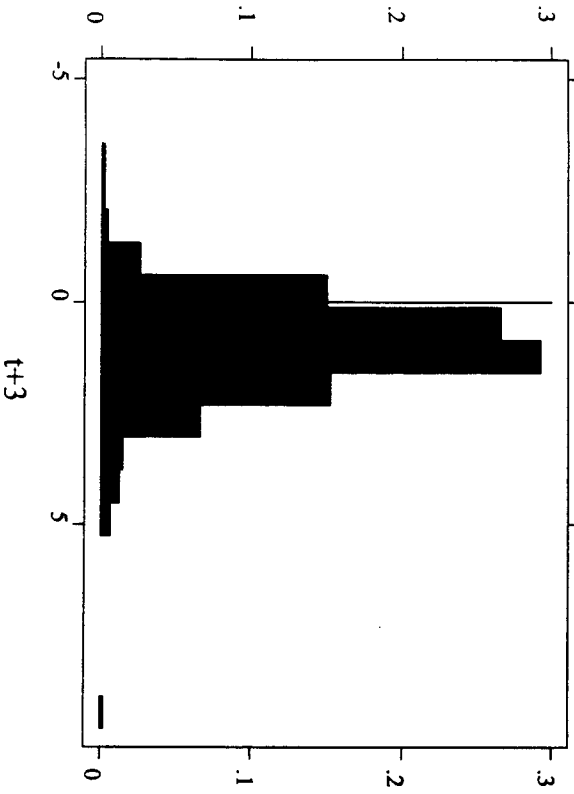
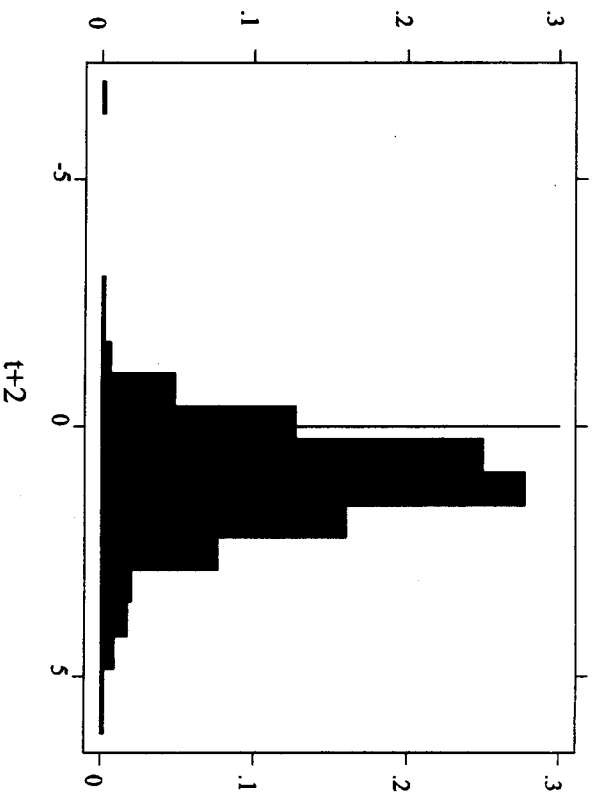
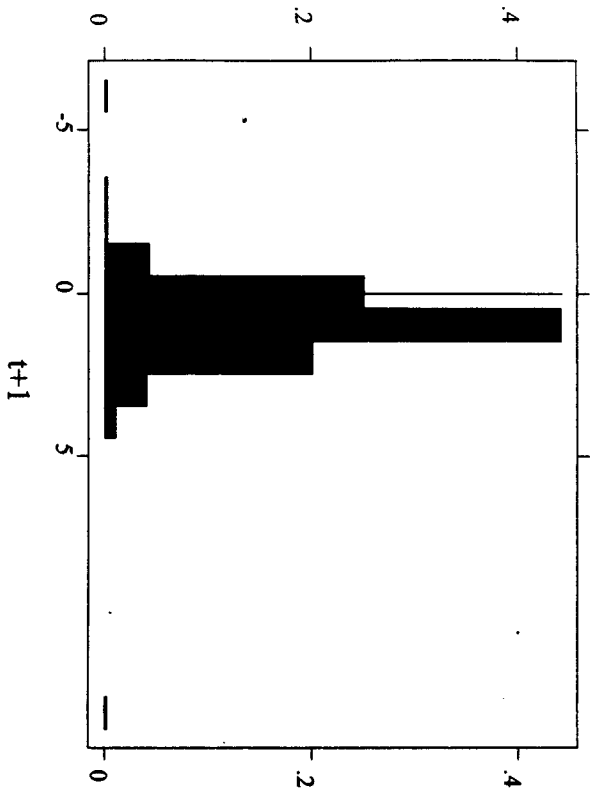
Data Source: NBER 458 Manufacturing Industries Database from 1958 to 1992

## PREDICTING INVESTMENT

Variable	Obs	Mean	Std. Dev.	Min	Max
b <sub>1</sub>	458	0.91236	1.139383	-6.55743	13.4523
b <sub>2</sub>	458	1.092412	1.1239	-6.97798	6.158016
b <sub>3</sub>	458	1.028215	1.119888	-2.94143	9.642923
b <sub>4</sub>	458	0.987436	1.07193	-2.20407	6.03586

$$d_i = \left( \frac{\Delta K}{K} \right)_{t+j} - \frac{1}{2} \left[ \left( \frac{\Delta K}{K} \right)_{t-1} + \left( \frac{\Delta K}{K} \right)_t \right]$$

$$d_i = a + b_j \Delta TFP_t + e$$



## Distribution of Coefficient for Rate of Investment

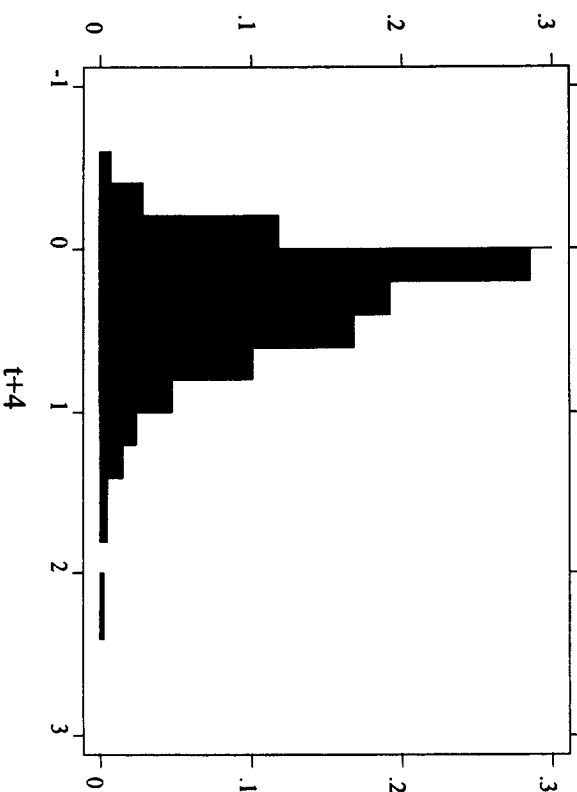
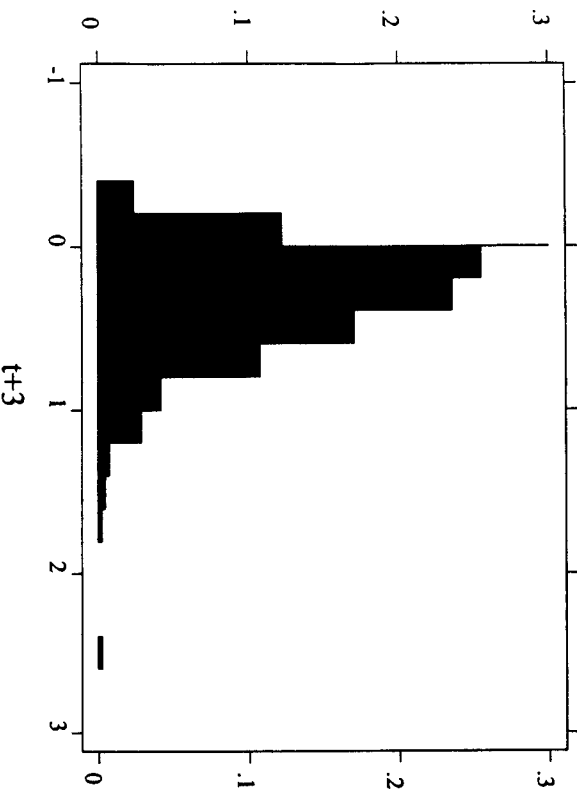
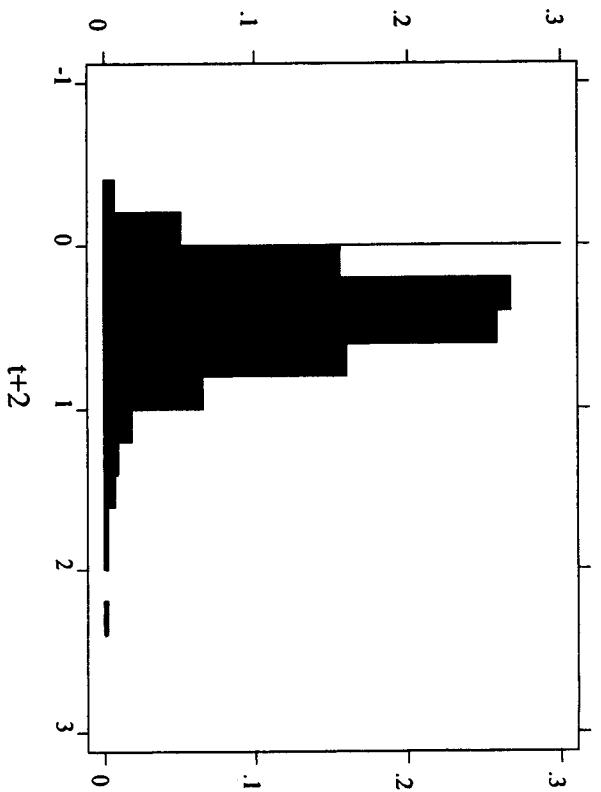
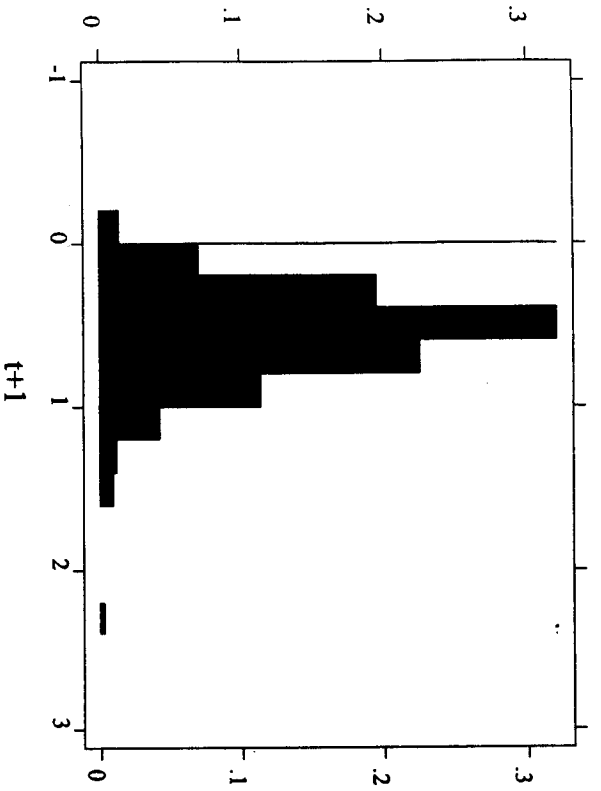
Data Source: NBER 458 Manufacturing Industries Database from 1958 to 1992

## PREDICTING OUTPUT

Variable	Obs	Mean	Std. Dev.	Min	Max
b <sub>1</sub>	458	0.559539	0.287642	-0.11916	2.201468
b <sub>2</sub>	458	0.439059	0.320583	-0.26786	2.320151
b <sub>3</sub>	458	0.333137	0.341268	-0.37061	2.410413
b <sub>4</sub>	458	0.334917	0.376029	-0.45452	2.307526

$$dY_j = \frac{Y_{t+j} - Y_{t-1}}{2}$$

$$dY_j = a + b_j \Delta TFP_t + e_t$$



## Distribution of Coefficient for Output

Data Source: NBER 458 Manufacturing Industries Database from 1958 to 1992

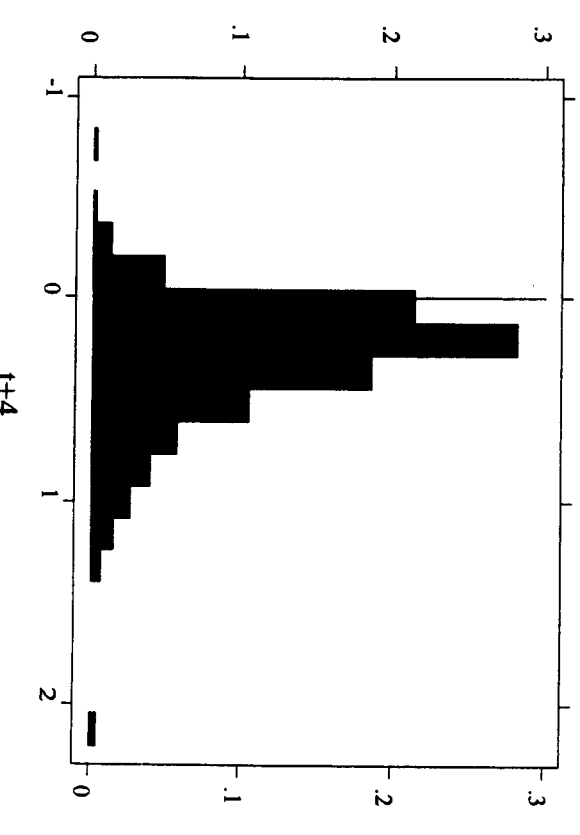
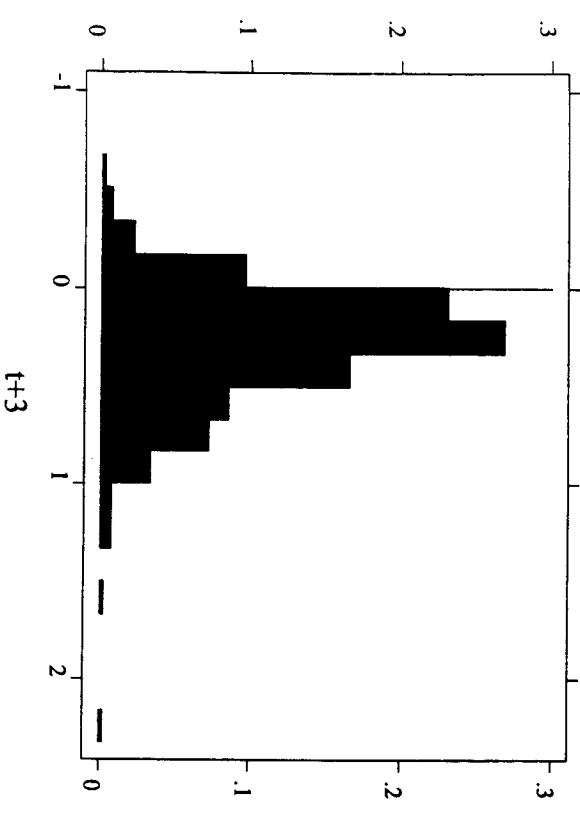
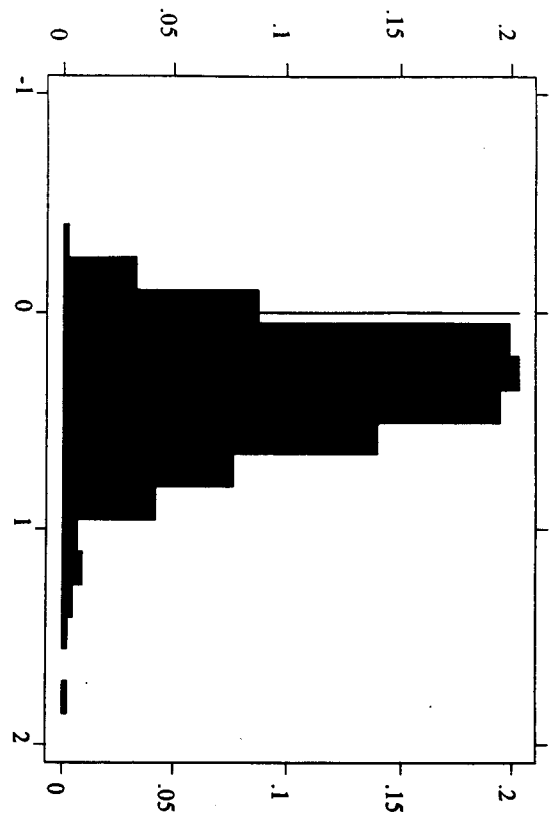
## PREDICTING EFFECTIVE LABOR

Variable	Obs	Mean	Std. Dev.	Min	Max
b <sub>1</sub>	458	0.355875	0.289515	-0.37769	1.78226
b <sub>2</sub>	458	0.336572	0.307729	-0.59494	1.792044
b <sub>3</sub>	458	0.291623	0.303515	-0.60827	2.331
b <sub>4</sub>	458	0.311044	0.321404	-0.681	2.203658

$$dL_j^* = \frac{L_j^*}{\left[ \frac{L_{t-1}^* + L_t^*}{2} \right]}$$

$$dL_j^* = a + b_j \Delta TFP_t + e$$





# Distribution of Coefficient for Effective Labor

Data Source: NBER 458 Manufacturing Industries Database from 1958 to 1992

- All the evidence confirms the existence of the “Growth Syndrome”.
- TFP improvement now pushes up the rate of return next year, and, by declining amounts, for at least three more years.
- The same is true for the investment rate, where the effect seems to be concentrated a bit farther into the future.
- The output effect also extends for at least four years and is more steady through time.
- And finally, a substantial and lasting effect on labor use is indicated.

## Issues of Causality

- One question that many of you may have concerns the direction of causality and the extent of feedback.
- To check this we worked with panel data with fixed effect for each industry.
- When a variable was used as a predictor, four lags were employed.

	$R^2$	$R^2$	
TFP to $\rho$	.80	.06	$\rho$ to TFP
TFP to $(\Delta K^*/K^*)$	.21	.02	$(\Delta K^*/K^*)$ to TFP
TFP to Y	.87	.01	Y to TFP

Direction of Causality for 458 Manufacturing Industries from NBER data (1958-92). Reported  $R^2$ s are weighted adjusted  $R^2$ s.

CAUSALITY: TFP GROWTH RATES -> RATES OF RETURN

$$\rho_{i,t} = \alpha_i + \beta_1 \Delta TFP_{i,t-1} + \beta_2 \Delta TFP_{i,t-2} + \beta_3 \Delta TFP_{i,t-3} + \beta_4 \Delta TFP_{i,t-4} + \varepsilon$$

Dependent Variable: RHO?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 18:21  
 Sample: 1963 1994  
 Included observations: 32  
 Total panel (balanced) observations 14656

Variable	Coefficient	Std. Error	t-Statistic	Prob.
TDTFP?(-1)	0.099175	0.002420	40.98931	0.0000
TDTFP?(-2)	0.074317	0.002441	30.44276	0.0000
TDTFP?(-3)	0.046838	0.002468	18.98015	0.0000
TDTFP?(-4)	0.038828	0.002452	15.83485	0.0000
Fixed Effects				
Weighted Statistics				
R-squared	0.806616	Mean dependent var		0.185719
Adjusted R-squared	0.800336	S.D. dependent var		0.111985
S.E. of regression	0.050039	Sum squared resid		35.54054
F-statistic	19734.71	Durbin-Watson stat		0.876900
Prob(F-statistic)	0.000000			
Unweighted Statistics				
R-squared	0.796403	Mean dependent var		0.141161
Adjusted R-squared	0.789791	S.D. dependent var		0.109260
S.E. of regression	0.050094	Sum squared resid		35.61908
Durbin-Watson stat	0.599004			

CAUSALITY: RATES OF RETURN-> TFP GROWTH RATES

$$\Delta TFP_{i,t} = \alpha_i + \beta_1 \rho_{i,t-1} + \beta_2 \rho_{i,t-2} + \beta_3 \rho_{i,t-3} + \beta_4 \rho_{i,t-4} + \varepsilon$$

Dependent Variable: TDTFP?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 18:25  
 Sample: 1962 1994  
 Included observations: 33  
 Total panel (balanced) observations 15113

Variable	Coefficient	Std. Error	t-Statistic	Prob.
RHO?(-1)	-0.559919	0.024364	-22.98109	0.0000
RHO?(-2)	-0.084488	0.030630	-2.758376	0.0058
RHO?(-3)	0.104068	0.030154	3.451225	0.0006
RHO?(-4)	0.109101	0.023242	4.694021	0.0000
<b>Fixed Effects</b>				
<b>Weighted Statistics</b>				
R-squared	0.090108	Mean dependent var		0.017039
Adjusted R-squared	0.061478	S.D. dependent var		0.124080
S.E. of regression	0.120206	Sum squared resid		211.6982
F-statistic	483.6357	Durbin-Watson stat		2.025027
Prob(F-statistic)	0.000000			
<b>Unweighted Statistics</b>				
R-squared	0.080295	Mean dependent var		0.014240
Adjusted R-squared	0.051357	S.D. dependent var		0.123784
S.E. of regression	0.120563	Sum squared resid		212.9600
Durbin-Watson stat	2.183746			

CAUSALITY: TFP GROWTH RATES -> RATES OF INVESTMENT

$$INVRAT_{i,t} = \alpha_i + \beta_1 \Delta TFP_{i,t-1} + \beta_2 \Delta TFP_{i,t-2} + \beta_3 \Delta TFP_{i,t-3} + \beta_4 \Delta TFP_{i,t-4} + \varepsilon$$

Dependent Variable: INVRAT?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 18:23  
 Sample: 1963 1994  
 Included observations: 32  
 Total panel (balanced) observations 14656

Variable	Coefficient	Std. Error	t-Statistic	Prob.
TDFP?(-1)	0.043750	0.003260	13.41996	0.0000
TDFP?(-2)	0.055114	0.003303	16.68533	0.0000
TDFP?(-3)	0.065662	0.003345	19.63083	0.0000
TDFP?(-4)	0.043373	0.003318	13.07087	0.0000
<b>Fixed Effects</b>				
<b>Weighted Statistics</b>				
R-squared	0.235379	Mean dependent var		0.023289
Adjusted R-squared	0.210545	S.D. dependent var		0.054948
S.E. of regression	0.048822	Sum squared resid		33.83320
F-statistic	1456.478	Durbin-Watson stat		1.194864
Prob(F-statistic)	0.000000			
<b>Unweighted Statistics</b>				
R-squared	0.191813	Mean dependent var		0.021060
Adjusted R-squared	0.165564	S.D. dependent var		0.053539
S.E. of regression	0.048906	Sum squared resid		33.94942
Durbin-Watson stat	1.112492			

CAUSALITY: RATES OF INVESTMENT-> TFP GROWTH RATES

$$\Delta TFP_{i,t} = \alpha_i + \beta_1 INVRAT_{i,t-1} + \beta_2 INVRAT_{i,t-2} + \beta_3 INVRAT_{i,t-3} + \beta_4 INVRAT_{i,t-4} + \epsilon$$

Dependent Variable: TDTFP?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 18:18

Sample: 1953 1994  
 Included observations: 32  
 Total panel (balanced) observations 14655

Variable	Coefficient	Std. Error	t-Statistic	Prob.
INVRAT?(-1)	-0.337854	0.017866	-18.91038	0.0000
INVRAT?(-2)	0.025054	0.018725	1.337986	0.1809
INVRAT?(-3)	-0.025363	0.017469	-1.451897	0.1466
INVRAT?(-4)	-0.051284	0.016328	-3.140948	0.0017
Fixed Effects				
Weighted Statistics				
R-squared	0.048265	Mean dependent var		0.015040
Adjusted R-squared	0.017351	S.D. dependent var		0.124927
S.E. of regression	0.123839	Sum squared resid		217.6647
F-statistic	239.9193	Durbin-Watson stat		2.188214
Prob(F-statistic)	0.000000			
Unweighted Statistics				
R-squared	0.042057	Mean dependent var		0.012826
Adjusted R-squared	0.010942	S.D. dependent var		0.124700
S.E. of regression	0.124016	Sum squared resid		218.2876
Durbin-Watson stat	2.292250			



CAUSALITY: TFP GROWTH RATES -> OUTPUT

$$Y_{i,t} = \alpha_i + \beta_1 \Delta TFP_{i,t-1} + \beta_2 \Delta TFP_{i,t-2} + \beta_3 \Delta TFP_{i,t-3} + \beta_4 \Delta TFP_{i,t-4} + \varepsilon$$

Dependent Variable: GDPDF?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 18:58  
 Sample: 1963 1994  
 Included observations: 32  
 Total panel (balanced) observations 14656

Variable	Coefficient	Std. Error	t-Statistic	Prob.
TDTFP?(-1)	232.5733	13.17454	17.65323	0.0000
TDTFP?(-2)	170.0432	13.44903	12.64353	0.0000
TDTFP?(-3)	111.9923	13.63771	8.211954	0.0000
TDTFP?(-4)	75.74750	13.42035	5.644225	0.0000
<b>Fixed Effects</b>				
<b>Weighted Statistics</b>				
R-squared	0.875480	Mean dependent var	5104.203	
Adjusted R-squared	0.871436	S.D. dependent var	3032.534	
S.E. of regression	1087.340	Sum squared resid	1.68E+10	
F-statistic	33265.31	Durbin-Watson stat	0.413625	
Prob(F-statistic)	0.000000			
<b>Unweighted Statistics</b>				
R-squared	0.896097	Mean dependent var	2215.810	
Adjusted R-squared	0.892723	S.D. dependent var	3484.838	
S.E. of regression	1141.396	Sum squared resid	1.85E+10	
Durbin-Watson stat	0.217448			

CAUSALITY: RATES OF RETURN-> TFP GROWTH RATES

$$\Delta TFP_{i,t} = \alpha_i + \beta_1 Y_{i,t-1} + \beta_2 Y_{i,t-2} + \beta_3 Y_{i,t-3} + \beta_4 Y_{i,t-4} + \varepsilon$$

Dependent Variable: TDTFP?  
 Method: GLS (Cross Section Weights)  
 Date: 12/09/99 Time: 19:05  
 Sample: 1962 1994  
 Included observations: 33  
 Total panel (balanced) observations 15113

Variable	Coefficient	Std. Error	t-Statistic	Prob.
GDPDF?(-1)	-1.97E-05	1.74E-06	-11.33221	0.0000
GDPDF?(-2)	-4.57E-06	2.46E-06	-1.854078	0.0637
GDPDF?(-3)	3.64E-06	2.49E-06	1.461663	0.1439
GDPDF?(-4)	1.24E-05	1.78E-06	6.980988	0.0000
Fixed Effects				
Weighted Statistics				
R-squared	0.043927	Mean dependent var		0.017033
Adjusted R-squared	0.013844	S.D. dependent var		0.124362
S.E. of regression	0.123499	Sum squared resid		223.4555
F-statistic	224.3833	Durbin-Watson stat		2.155580
Prob(F-statistic)	0.000000			
Unweighted Statistics				
R-squared	0.033716	Mean dependent var		0.014240
Adjusted R-squared	0.003312	S.D. dependent var		0.123784
S.E. of regression	0.123579	Sum squared resid		223.7455
Durbin-Watson stat	2.273131			

- Now, we turn to a comparison of the 2-Deflator and the Traditional Methods using the NBER data set. The basic data are simple correlations between  $\Delta TFP$  in period  $t$  with  $\Delta Y$ ,  $\Delta VA$ ,  $\Delta K$ , and  $\Delta L$ , both contemporaneously and for periods  $t+1$ ,  $t+2$ , and  $t+3$ .

- We record in the following tables the number of cases (out of 458) in which the correlation in question was positive. In each table the “same” story is told four times:

$\Delta TFP^*$  to  $\Delta Y^*$

$\Delta TFP^*$  to  $\Delta Y$

$\Delta TFP$  to  $\Delta Y^*$

$\Delta TFP$  to  $\Delta Y$

- The first table goes from  $\Delta\text{TFP}$  to output, the second from  $\Delta\text{TFP}$  to  $\Delta\text{Value added}$ , the third from  $\Delta\text{TFP}$  to investment, the fourth from  $\Delta\text{TFP}$  to labor force, and the fifth from  $\Delta\text{TFP}$  to  $(\rho+\delta)$ .
- The bottom line is that all the stories are basically the same. In particular,  $\Delta\text{TFP}^*$  is just about as good a “predictor” of  $\Delta Y$  as it is of  $\Delta Y^*$ , and  $\Delta\text{TFP}$  is just about as good a predictor of  $\Delta Y^*$  as it is of  $\Delta Y$ . Equally,  $\Delta\text{TFP}^*$  predicts  $\Delta\text{VA}$  as well as  $\Delta\text{VA}^*$ , and  $\Delta N$  nearly as well as  $\Delta L^*$ .

- This tells us that the difference in methods of calculation of TFP is not the source of any major difference in results. Potential bias due to change in relative price being in both  $\Delta TFP^*$  and  $\Delta Y^*$  and in both  $\Delta TFP^*$  and  $\Delta VA^*$  do not seem to matter.  $\Delta TFP^*$  is good at predicting even when the “predictand” is  $\Delta Y$  or  $\Delta VA$ , neither of which contains a price-change element.

TFP GROWTH RATE AS A PREDICTOR OF OUTPUT  
(CORRELATIONS BETWEEN  $\Delta TFP$  AND  $\Delta Y$ )

	$\Delta TFP^*_t$ (2-Deflator) # of Positive Correlations	$\Delta TFP_t$ (Traditional) # of Positive Correlations
$\Delta Y^*_t$	411	431
$\Delta Y^*_{t+1}$	306	281
$\Delta Y^*_{t+2}$	155	168
$\Delta Y^*_{t+3}$	145	169
$\Delta Y_t$	448	455
$\Delta Y_{t+1}$	282	285
$\Delta Y_{t+2}$	140	155
$\Delta Y_{t+3}$	151	178

Note: All results are significant at least at 0.0002 level.

TFP GROWTH RATE AS A PREDICTOR OF VALUE ADDED  
(CORRELATIONS BETWEEN  $\Delta TFP$  AND  $\Delta VA$ )

	$\Delta TFP^*_t$ (2-Deflator) # of Positive Correlations	$\Delta TFP_t$ (Traditional) # of Positive Correlations
$\Delta VA^*_t$	458 •	447 •
$\Delta VA^*_{t+1}$	245	234
$\Delta VA^*_{t+2}$	124 •	155 •
$\Delta VA^*_{t+3}$	245	181 •
$\Delta VA_t$	449 •	458 •
$\Delta VA_{t+1}$	215	246
$\Delta VA_{t+2}$	147 •	142 •
$\Delta VA_{t+3}$	150 •	175 •

Note : “•” results are significant at least at 0.0008 level.



TFP GROWTH RATE AS A PREDICTOR OF INVESTMENT  
(CORRELATIONS BETWEEN  $\Delta TFP$  AND  $\Delta K$ )

	$\Delta TFP^*_t$ (2-Deflator) # of Positive Correlations	$\Delta TFP_t$ (Traditional) # of Positive Correlations
$\Delta K^*_t$	300 •	347 •
$\Delta K^*_{t+1}$	358 •	324 •
$\Delta K^*_{t+2}$	299 •	286 •
$\Delta K^*_{t+3}$	241	259
$\Delta K_t$	121 •	154 •
$\Delta K_{t+1}$	296 •	269 •
$\Delta K_{t+2}$	339 •	313 •
$\Delta K_{t+3}$	314	287 •

Note: “•” results are significant at least at 0.0001 level.

TFP GROWTH RATE AS A PREDICTOR OF LABOR  
(CORRELATIONS BETWEEN  $\Delta$ TFP AND  $\Delta$ L)

	$\Delta$ TFP* <sub>t</sub> (2-Deflator) # of Positive Correlations	$\Delta$ TFP <sub>t</sub> (Traditional) # of Positive Correlations
$\Delta L^*_t$	402 •	423 •
$\Delta L^*_{t+1}$	356 •	311 •
$\Delta L^*_{t+2}$	269	230
$\Delta L^*_{t+3}$	205	219
$\Delta L_t$	416 •	402 •
$\Delta L_{t+1}$	348 •	337 •
$\Delta L_{t+2}$	203	200
$\Delta L_{t+3}$	188	217

Note: "•" results are significant at least at 0.0001 level.

- Finally, we come to the prediction of the gross rate of return ( $\rho+\delta$ ). Here we only have the rate of return from the 2-Deflator Method. But we can see once again that we can predict it just about equally well starting from  $\Delta TFP$  or from  $\Delta TFP^*$

TFP GROWTH RATE AS A PREDICTOR OF GROSS RATES OF  
RETURN  
(CORRELATIONS BETWEEN  $\Delta TFP$  AND  $(\rho+\delta)$ )

	$\Delta TFP^*_t$ (2-Deflator) # of Positive Correlations	$\Delta TFP_t$ (Traditional) # of Positive Correlations
$(\rho+\delta)_t$	453	389
$(\rho+\delta)_{t+1}$	435	366
$(\rho+\delta)_{t+2}$	399	322
$(\rho+\delta)_{t+3}$	304	267

Note: All results are significant at least at 0.0001 level.

- Now, we turn to yet another data set – the U.N. Industrial Statistics, broken down into 3-digit manufacturing sectors. Here the calculations were made for four industrialized countries, four rapid growers from East Asia, and four Latin American countries.
- Here we only can use the 2-Deflator Method, as we do not have breakdowns of value added into price and quantity components.
- But we are doing the same kind of predicting we did earlier using the NBER data set.

- The next table takes as its “predictand” the changes in the net rate of return from time  $[(t + t-1) / 2]$  to time  $t+j$ . Our prediction of positive correlations is amply confirmed. (The 4 cases with less than 50% positive correlations are underlined; note that 3 of them are for period  $t+4$ .)

23 APR 14 REEDITION % of GDP from  $P_t + P_{t+1}$   
 (percentage of GDP)

	$P_{t+1} - (P_t + P_{t+1})/2$	$P_{t+2} - (P_t + P_{t+1})/2$	$P_{t+3} - (P_t + P_{t+1})/2$	$P_{t+4} - (P_t + P_{t+1})/2$
Canada	89.3%	82.1%	42.9%	25.0%
USA	92.9%	67.9%	60.7%	89.3%
Japan	100.0%	88.9%	100.0%	96.3%
UK	89.3%	85.7%	78.6%	89.3%
Indonesia	88.0%	64.0%	60.0%	64.0%
Korea	92.9%	82.1%	67.9%	78.6%
Malaysia	82.1%	78.6%	64.3%	50.0%
Philippines	89.3%	89.3%	89.3%	57.1%
Chile	92.9%	85.7%	75.0%	67.9%
Colombia	64.3%	60.7%	53.6%	46.4%
Mexico	53.8%	73.1%	65.4%	42.3%
Panama	84.0%	84.0%	72.0%	72.0%
Average	84.9%	78.5%	69.1%	64.8%

**Correlations between Contemporaneous TFP Growth Rate and Rates of Return for Three Digit Manufacturing Sectors from U.N. Industrial Statistics**

- There follows a series of graphs which consolidate the results for the 12 countries. Please recall that all the basic regressions are within one 3-digit industry within one country.
- The histograms show how many individual correlations lie between 0.1 and 0.2, between 0.2 and 0.3, etc. Positive correlations are reflected in green and negative ones in red.



- In the four graphs, we have  $\Delta TFP$  at time  $t$  being used to “predict” differences up to 4 periods ahead in

$$\rho^*_{t+j} - \frac{(\rho^*_{t-1} + \rho^*_t)}{2}$$

$$\left[ \frac{Y^*_{t+j}}{Y^*_{t-1} + Y^*_t} \right]$$

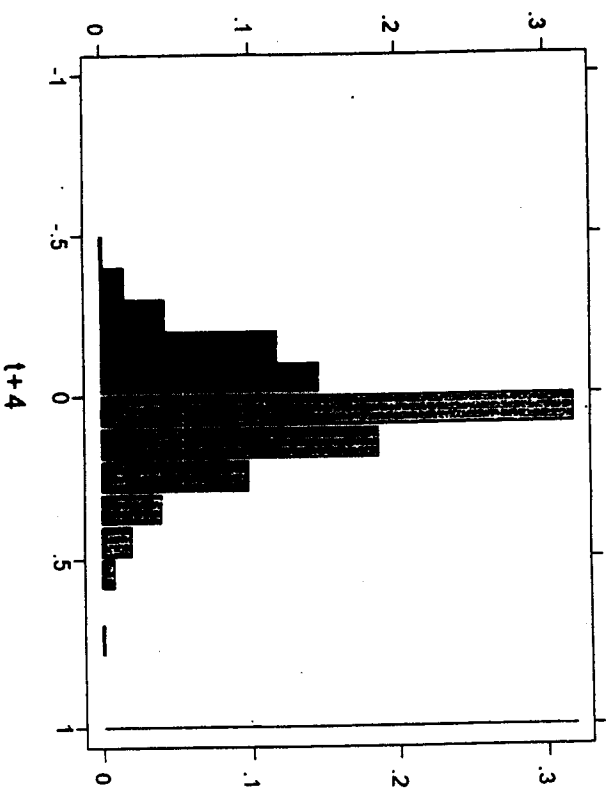
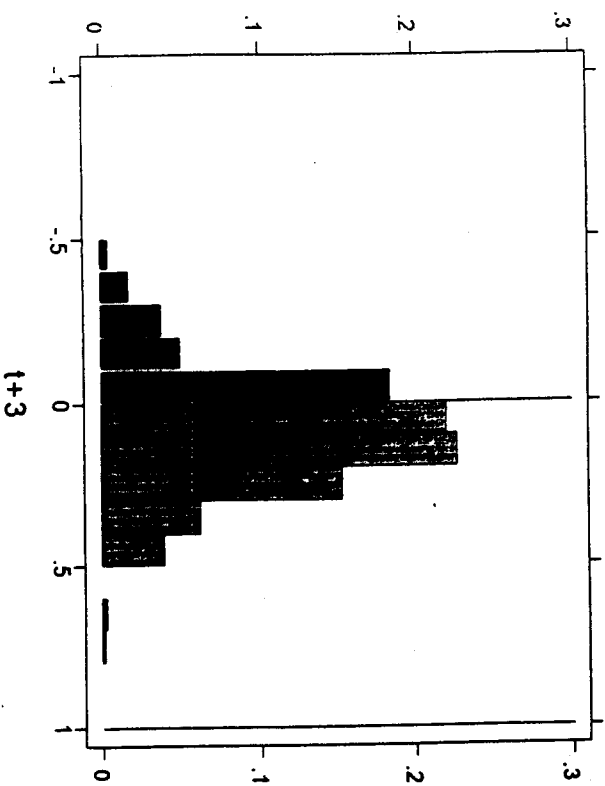
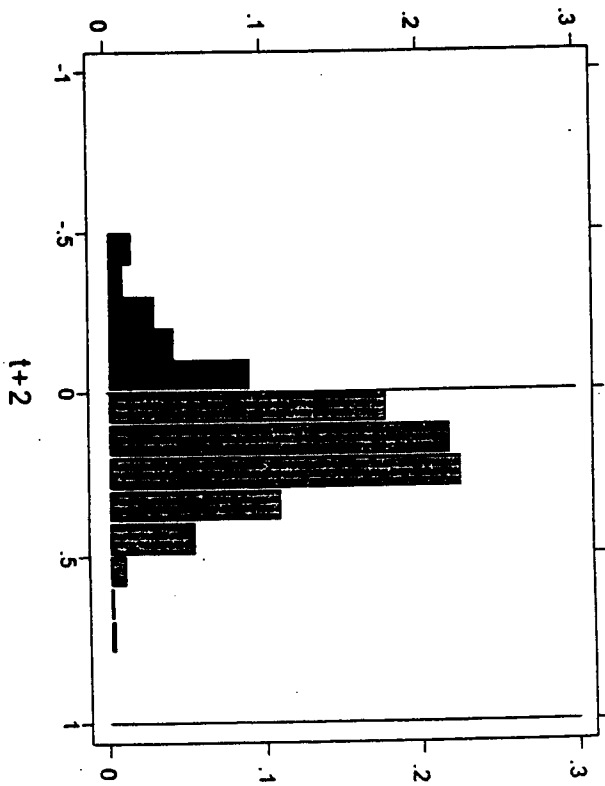
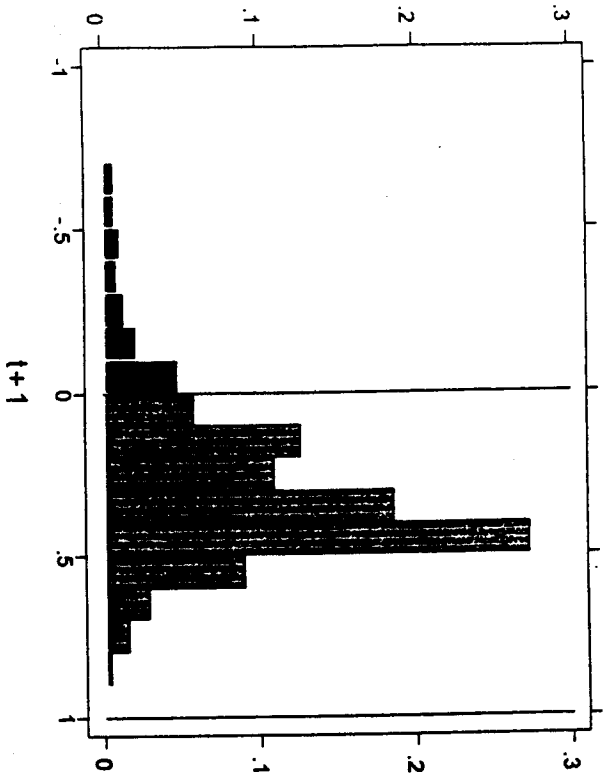
$$\left[ \frac{K^*_{t+j}}{K^*_{t-1} + K^*_t} \right]$$

$$\left( \frac{I^*}{K^*} \right)_{t+j} - \frac{\left( \left( \frac{I^*}{K^*} \right)_{t-1} + \left( \frac{I^*}{K^*} \right)_t \right)}{2}$$

$$\left[ \frac{L^*_{t+j}}{L^*_{t-1} + L^*_t} \right]$$

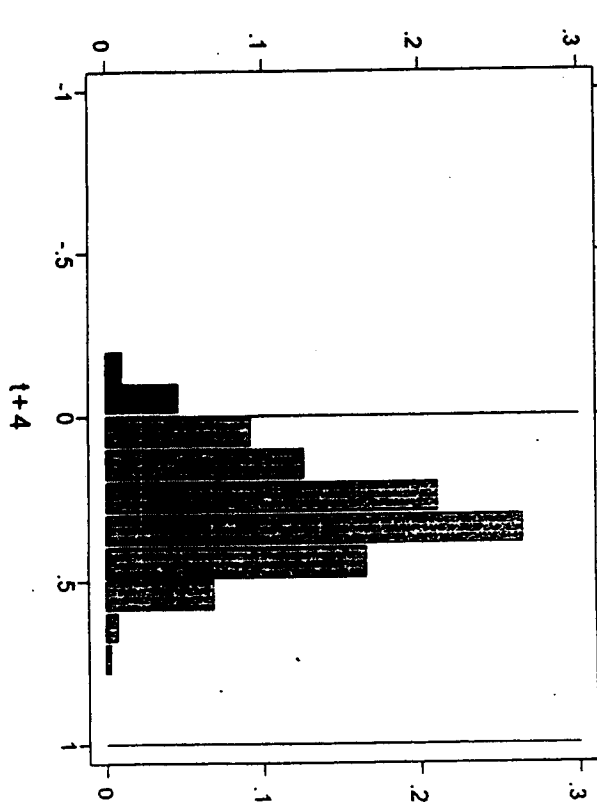
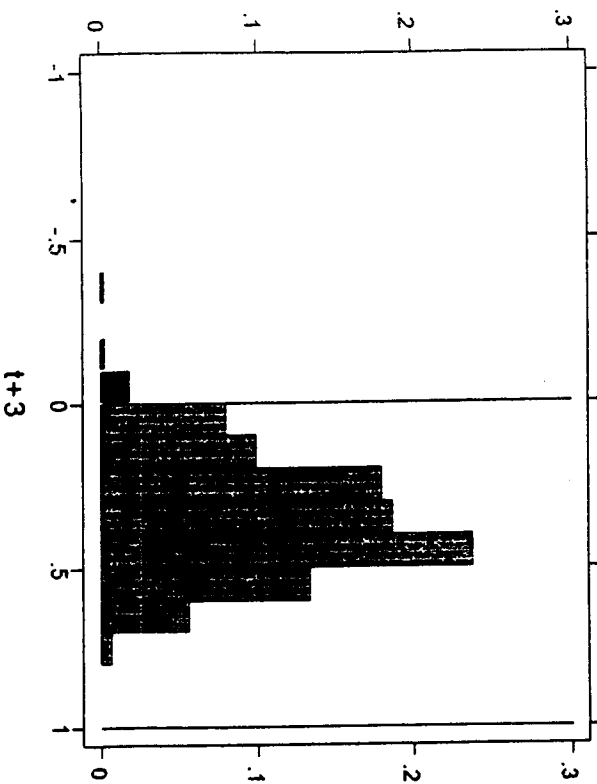
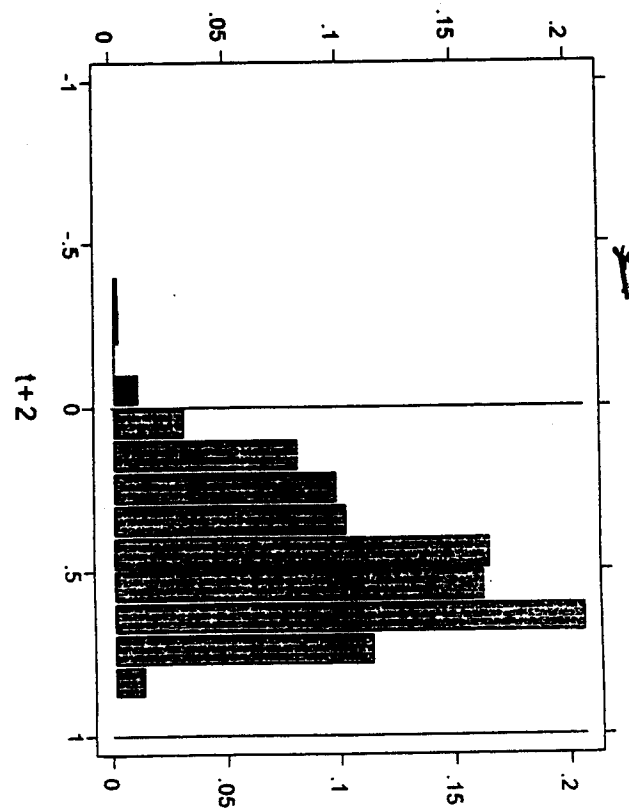
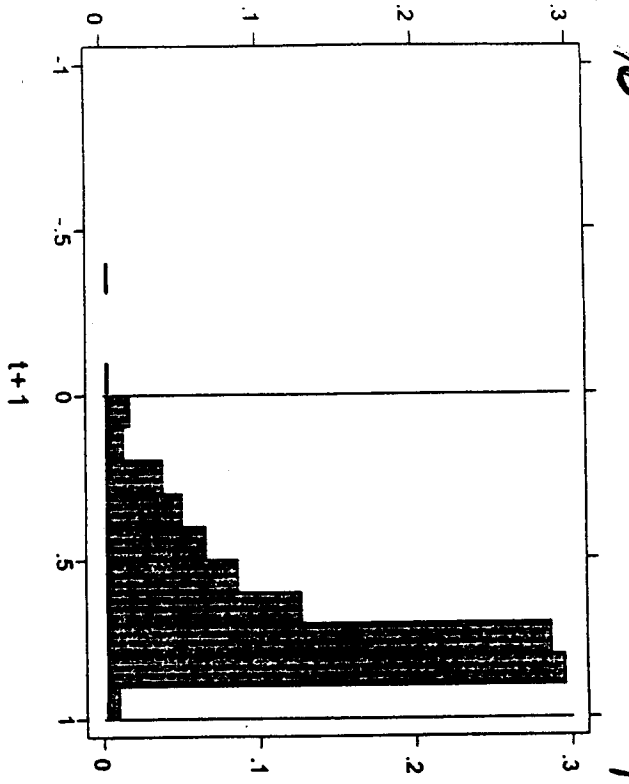
- Once again we find confirmation of our “syndrome” of real cost reduction followed by higher rates of profit, increased investment, increased output, and even (in this case) increased use of labor.

% ΔTFP PREDICTIONS % Δ P<sub>t</sub> from  $\frac{P_{t-1} + P_t}{2}$



U.N.: Correlation between TFP and Rate of Return  
CORRELATIONS ARE WITHIN SECTORS FOR EACH COUNTRY

% ATTP increasing DFF from  $\frac{-1}{2} + \frac{-1}{2} + \frac{1}{2}$



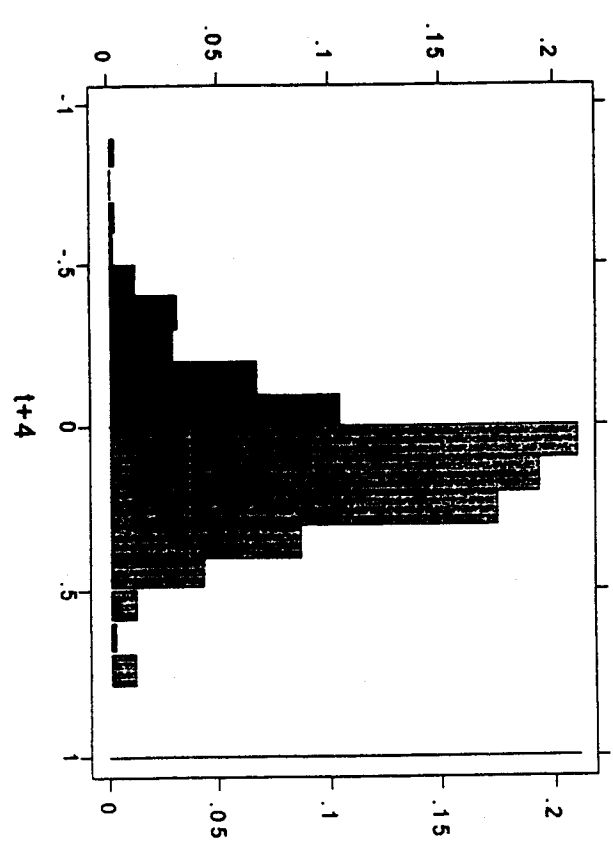
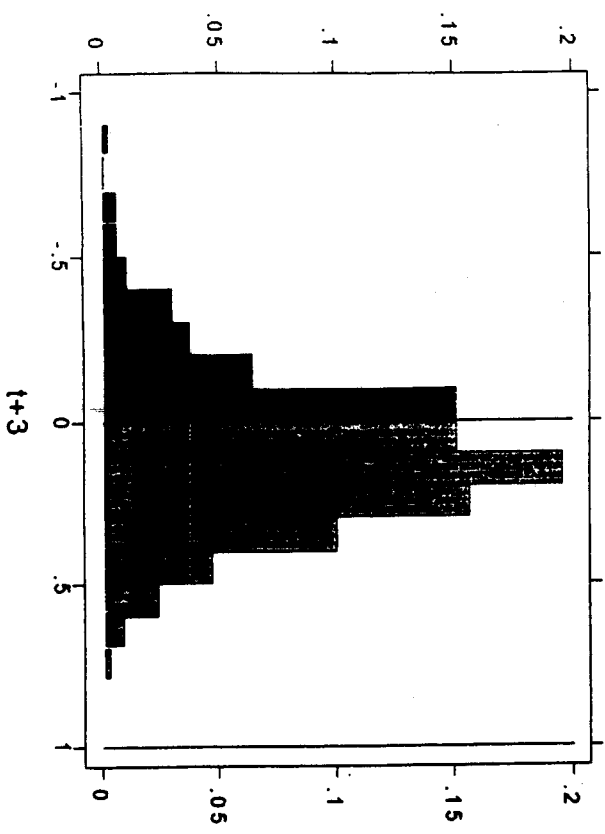
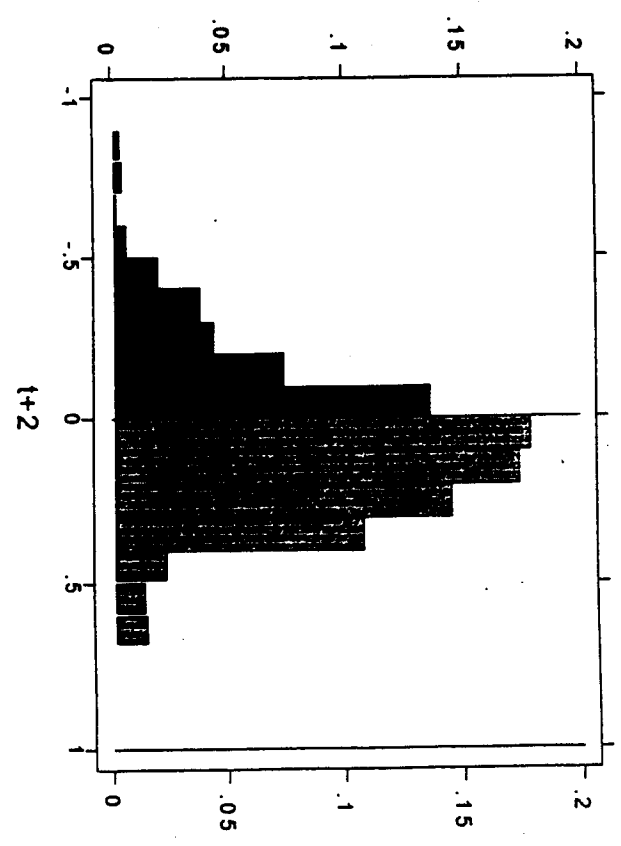
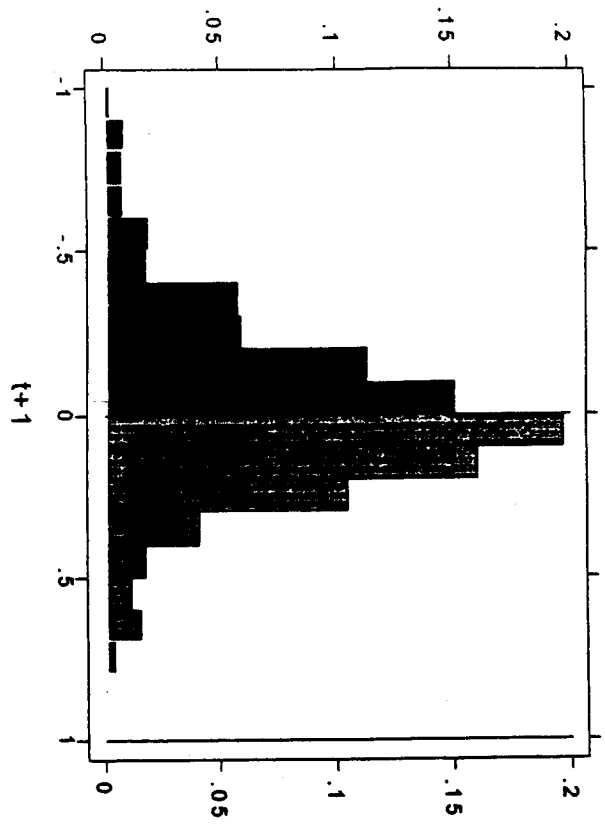
U.N.: Correlation between TFP and Output

CORRELATIONS ARE WITHIN SECTORS FOR EACH COUNTRY





50% A111111 PREDICTIVE % AK FROM K<sub>t-1</sub> + K<sub>t-2</sub>

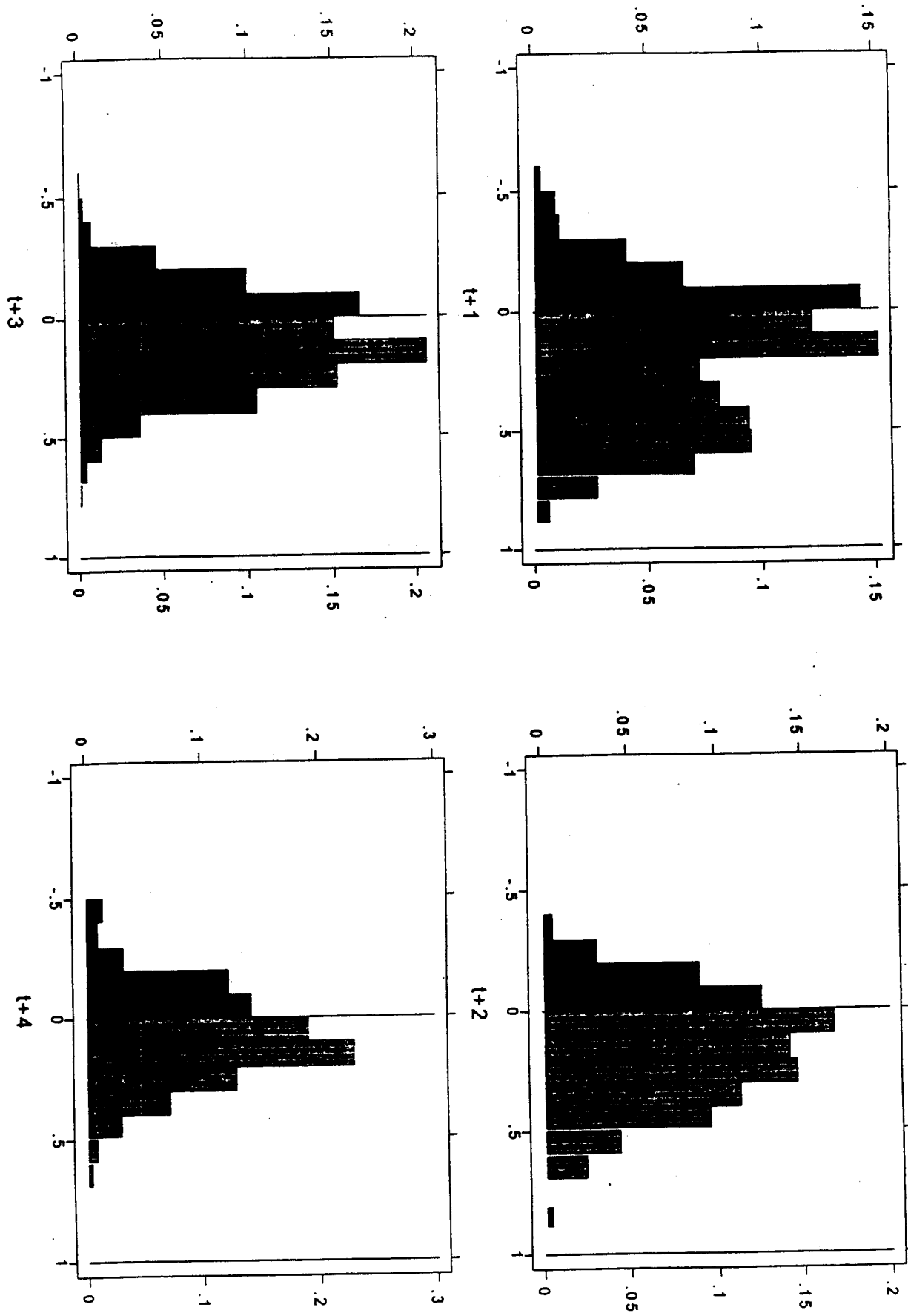


### U.N.: Correlation between TFP and Capital Stock

CORRELATIONS ARE WITHIN SECTORS FOR EACH COUNTRY



1/5 A1 E P T PREDICTING % AI FROM  $I_{t-1} + I_t$

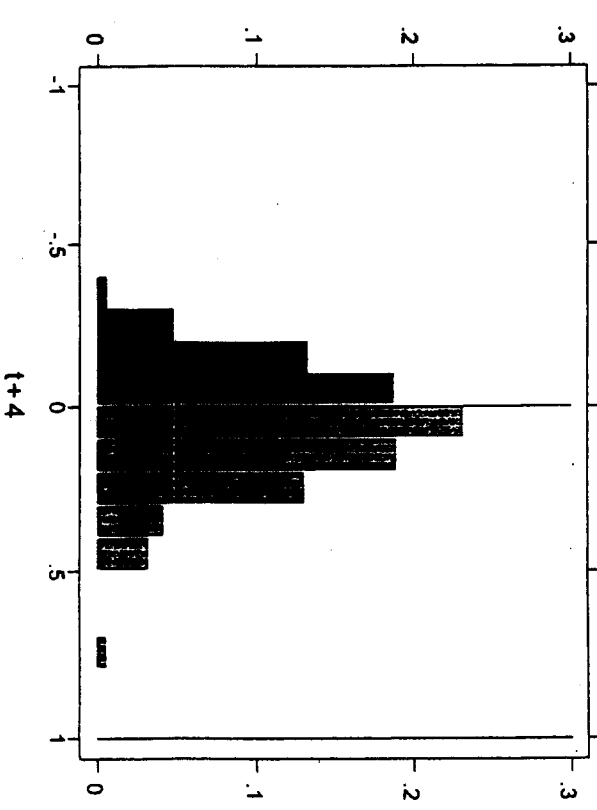
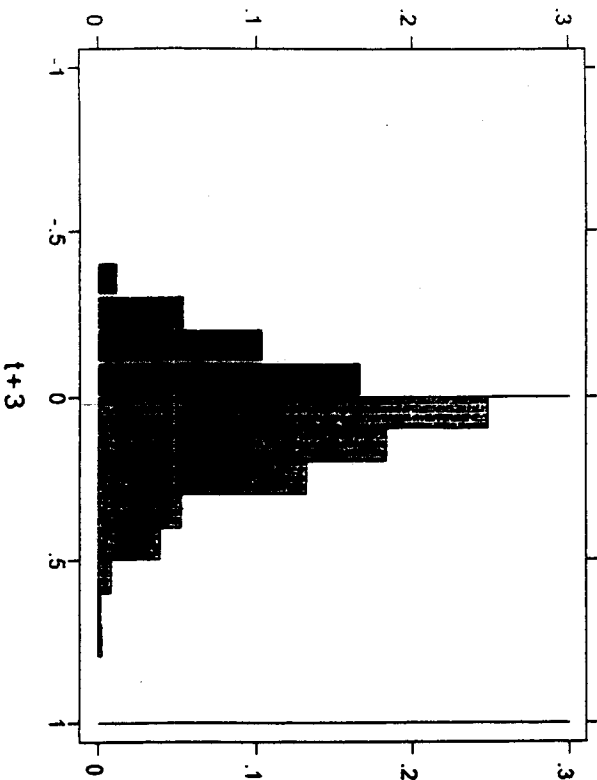
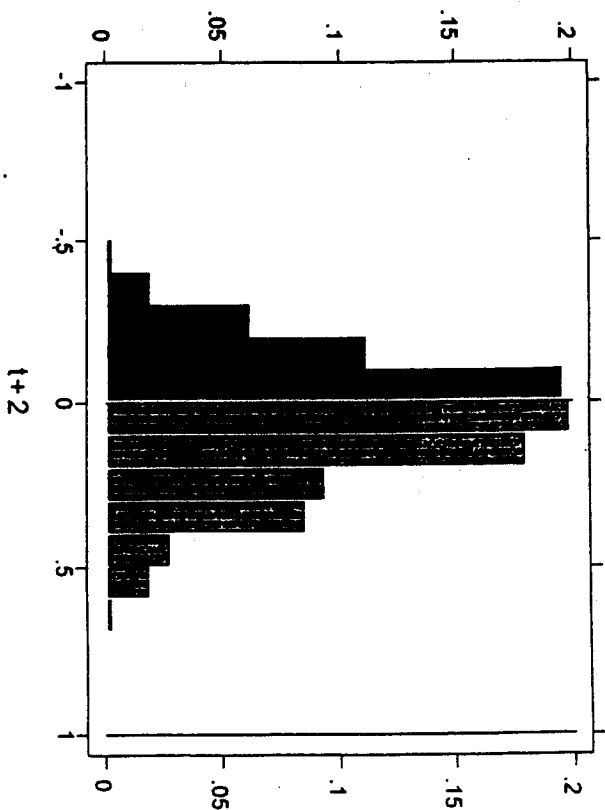
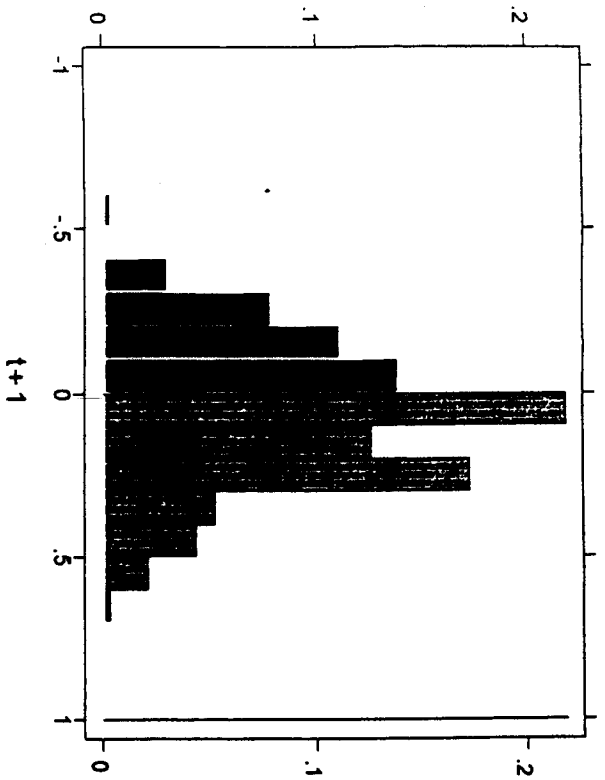


U.N.: Correlation between TFP and Investment

COMPARISONS ARE WITHIN SECTORS FOR EACH COUNTRY



% A1FR6 PREDICTIONS % D04 PVA = ESTIMATES



U.N.: Correlation between TFP and Labor

CORRELATIONS ARE WITHIN SECTORS FOR EACH COUNTRY

PREDICTING CHANGES IN RATES OF RETURN  
IN KOREA AND JAPAN

$$(\Delta TFP_t, \text{PREDICTING } \left[ \rho^*_{t+j} - \frac{(\rho^*_{t-1} + \rho^*_t)}{2} \right])$$

	Number of Positive Correlations (Sign Test)			
	t+1	t+2	t+3	t+4
59 Industries	54	40	35	38
3-digit Korea	(6.4)**	(2.7)**	(1.4)	(2.2)*
139 Industries	119	103	81	74
4-digit Korea	(8.4)**	(5.7)**	(2.0)	(0.8)
139 Firms	111	87	79	77
Korea	(7.0)**	(3.0)**	(1.6)	(1.3)
167 Firms	151	151	108	97
Japan	(10.4)**	(10.4)**	(3.8)**	(2.1)*

- 1) The value of sign test is  $Z = (x - np) / (npq)^{1/2}$ , where x is the number of positive correlations, n is the total number of observations (firms or industries), and  $p = q = 1/2$ .
- 2) Korea industries: 1976-96, Korea Firms: 1986-96, Japan Firms: 1977-1996

\* significant at the 0.05 level.  
\*\* significant at the 0.01 level.



- Our final table presents data from Korea and Japan. Here we once again take  $\Delta TFP_t$  as the

predictor and  $\left[ \rho_{t+j}^* - \frac{(\rho_{t-1}^* + \rho_t^*)}{2} \right]$  as our “predictand”.

- The data sets refer:
  - a) To 59 3-digit industries in Korea
  - b) To 139 4-digit industries in Korea
  - c) To 139 listed firms in Korea
  - d) To 167 listed firms in Japan

## PREDICTING CHANGES IN RATES OF RETURN IN KOREA AND JAPAN

$$(\Delta TFP_t \text{ PREDICTING } \left[ \rho^*_{t+j} - \frac{(\rho^*_{t-1} + \rho^*_t)}{2} \right])$$

	Number of Positive Correlations (Sign Test)			
	t+1	t+2	t+3	t+4
<b>59 Industries</b>	54	40	35	38
<b>3-digit Korea</b>	(6.4)**	(2.7)**	(1.4)	(2.2)*
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- \*\* significant at the 0.01 level.