## Economics 326: Suggested Solutions to Midterm 1

1 February, 2004

1. There are two equilibria. First, only low types trade and $p=8$. Second, low and medium types trade and $p=10.5$.
2. Suppose proportion $\pi$ are low quality.
(a) The equilibrium where only low types trade always exists.
(b) The equilibrium where both types trade exists if $20 \pi+30(1-\pi) \geq 25$. That is, $\pi \leq 1 / 2$.
3. Multiplicative reserve values:
(a) The expected quality, given price $p$, is $E[\theta \mid r(\theta) \leq p]=E[\theta \mid \theta \leq 4 p / 3]$. This equals $2 p / 3$ if $p \leq 3 / 4$, and $1 / 2$ if $p \geq 3 / 4$. Hence the unique equilibrium is $p=0$. There is complete unravelling.
(b) The expected quality, given price $p$, is $2 p$ if $p \leq 1 / 4$, and $1 / 2$ if $p \geq 1 / 4$. Hence there are two equilibria: $p=0$ and $p=1 / 2$. The latter seems more reasonable and is the only stable one.
