THE NBER INTERNATIONAL TRANSMISSION MODEL:

THE MARK II DISEQUILIBRIUM VERSION, ESTIMATES AND LESSONS

by

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This paper is an interim report on work in progress at the National Bureau of Economic Research aimed at modeling the international transmission of inflation through the world monetary system. It outlines the initial estimating version of the model (the Mark II version), presents the estimated model, and discusses the implications of these results for

*University of California, Los Angeles, and the National Bureau of Economic Research. This paper is a progress report through August 1978 on a portion of the NBER project on "The International Transmission of Inflation through the World Monetary System." My partners in this effort -- Arthur E. Gandolfi, James R. Lothian, Anna J. Schwartz, and Alan C. Stockman-- have made innumerable contributions to this modeling and created the NBER quarterly international data base used in estimating the model. In particular, Alan C. Stockman collaborated fully with the author on the estimation of the model and in formulating plans for the Mark III version. The author acknowledges the able research assistance of Daniel M. Laskar, Michael T. Melvin, and M. Holly Shissler and helpful comments and suggestions from members of the project Advisory Board and the UCLA Monetary Economics Workshop. This work has been funded by grants from the National Science Foundation (grant number APR76-12334), Scaife Family Trusts, Alex C. Walker Educational and Charitable Foundation, and Reim Foundation. This paper has not undergone the review accorded official NBER publications; in particular, it has not been submitted for approval by the Board of Directors and therefore is not a publication of the National Bureau.

1 An earlier report is contained in Darby (1977b).
a revised Mark III model and other empirical studies.\textsuperscript{2} The Mark II model is a quarterly macroeconometric model of Canada, France, Germany, Italy, Japan, the Netherlands, the United Kingdom, and the United States applied to data from 1955 through 1976.

The primary purpose of the model is to provide a means for measuring the relative importance of various channels by which inflation can be transmitted from country to country. We hope to identify how the relative importance of these channels has changed with changes in exchange rate regimes. This will provide information on the implications for inflation of alternative international monetary systems.

The Mark II model was proposed for the initial confrontation of the theoretical conceptions with the data set. We had no illusions that no major changes would result from this confrontation. As a result our work has been aimed at maximizing the information obtained as to what an acceptable model would look like. For this reason, we started with a consistent model of sufficient generality to let the data guide us in our revision although this model did not represent the single best guess of anyone on the project as to what the final model would look like. In addition, relatively simple, on-line, and inexpensive estimation techniques have been used. When we are satisfied with the specification of the model, it will be appropriate to utilize more sophisticated econometric techniques. The empirical results reported here are for the pooled period or the fixed exchange rate period only; the analysis of changes of exchange rate regimes awaits construction of the Mark III model. The Mark II model has proved a

\textsuperscript{2}Complete derivations and references for the individual equations of the final model will be contained in the planned volume reporting the results of the entire project.
very successful learning tool for those who have worked on it and we report those lessons here.

The Mark II model clearly distinguishes between the reserve-currency country (the United States) and all others. In Darby (1979) it is shown that in the long-run equilibrium, the world price level and inflation rate under fixed exchange rates are determined entirely within the reserve-currency country by its domestic demand for and supply of money. This is contrary to the heuristic arguments of Swooboda (1976) and others who attribute price level effects to domestic credit in proportion to country size. This long-run result does not preclude interesting short-run adjustments as variations in the U. S. inflation rate are transmitted through the international monetary system. It is also possible that reverse causation will occur as U. S. money supply and demand respond to short-run adjustments abroad. Under floating exchange rates, all countries are in effect reserve countries (except as they attempt to "stabilize" exchange rates) and a world inflation rate is no longer an appropriate concept.

The model is presented first in Sections I through III: In Section I, the U. S. submodel is presented with foreign variables treated as exogenous. Section II displays the standard nonreserve country submodel. Section III then explains how the submodels are integrated and highlights the parameters which indicate the importance of alternative channels by which inflation is transmitted. Section IV then examines the primarily econometric issues involved in the estimation of the model. Next the estimated equations and alternative forms are discussed in Section V. Finally plans for formulation of the Mark III version are developed in Section VI.
I. The U.S. Submodel

The U.S. submodel has two alternative forms, one corresponding to a fiat-reserve-currency country and the other to a commodity-reserve-currency country. One hypothesis which we wish to test is whether the U.S. shifted from a commodity to fiat standard in the early 1960s and whether this resulted in a worldwide inflation. For expository purposes, we will start with the simpler fiat case and then add the complications of the commodity case.

**Notation**

Capital letters are used to denote nominal (currency value) variables and lower case letters are used for real (deflated) variables. The variables will be defined as they are introduced and are collected for reference in Table 1. The subscript 1 is used to denote the United States and the subscripts 2 through 8 denote the other countries in our sample. All logarithms are taken with respect to the natural base e. Asterisks are used to indicate expected values formed in the previous period.
Overview

The U.S. (fiat) submodel consists of five equations and two identities which explain the endogenous variables real income $y_1$, price level $P_1$, nominal interest rate $R_1$, unemployment rate $u_1$, and nominal money supply, $M_1$.

The first four variables are explained in a relatively standard semi-reduced form model in which: (1) The long-run equilibrium values of real variables are unaffected by nominal variables. (2) Unanticipated variations in the nominal money supply, real government spending, strike activity, foreign real income, and foreign prices have transitory effects on domestic real variables.

A notable feature of the model is the endogeneity of the nominal money supply. This variable is determined via a monetary policy reaction function by unemployment, the price level, and interest rates.

Notably missing from both the list of endogenous variables and the monetary policy reaction function are the exchange rate and the balance of payments. The exchange rate for the reserve-currency country is identically equal to one. The balance of payments is irrelevant and ill-defined for a fiat-reserve-currency country. It might be defined formally as net foreign government purchases of U.S. securities, but this will not affect U.S. monetary policy as a gold flow would under a gold standard.

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3 That is the number of dollars per dollar $E_1 \equiv 1$.

4 We plan to test whether the U.S. monetary policy reaction function nonetheless showed a response to a balance-of-payments measure in the post-gold-standard era. Preliminary work by John Price (1978) suggests it did not.
We will now present the U.S. fiat submodel equation-by-equation and then summarize the discussion in tabular form.

The Price Level Equation

We use the same price level equation for both the reserve and nonreserve countries. In the case of nonreserve countries it is designed to test for the relative importance of direct price linkages; for the U.S. it captures both the influence of foreign price shocks and the possibility of reverse causation. The idea is that the price level is a weighted average of (1) the price level that would equate the domestic nominal supply of and demand for money and (2) the price level implied by complete international commodity arbitrage.

The price level implied by domestic monetary equilibrium is

\[ \log P_1 = \log M_1 - \log M_1^d \]

(1) \[ \log P_1 = \log M_1 - \left( \xi_{11} + \xi_{10} \xi_{12} t + \xi_{10} \xi_{13} \log y_1 + \xi_{10} \xi_{14} P_1 + (1-\xi_{10}) \log (M_{1t-1}/P_{1t-1}) + \sum_{i=1}^{4} w_i \hat{M}_1,t-i+1 \right) \]

where \( t \) is the time index and \( \hat{M}_1 \) is the innovation or unexpected portion of the nominal money supply measured as \( \log M_1 - (\log M_1) \). The short-run demand for money in square brackets is taken from Carr and Darby (1977). It combines a standard short-run demand for money with a transitory effect of monetary shocks on money demand similar to Darby (1972). We intend to experiment further with this specification, although it has performed well in preliminary estimations of equation (1).

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5 That is, to what extent does the "law of one price level" determine the price level?

The price level implied by complete international commodity arbitrage is measured in our model by the income-weighted index \( P^R_1 \) of prices in the other countries converted by the exchange rates into dollars per unit of output. The details of this calculation are given in Section III. Writers in the monetary approach to the balance of payments literature point out that \( P^R_1 \) may be multiplied by a constant factor of proportionality, but this goes into the constant term upon taking logarithms.

Upon combining equation (1) with \( \log P^R \) and simplifying the notation, the equation to be estimated is

\[
(2) \quad \log P_1 = \beta_{11} + T_1 \log P^R_1 + (1-T_1) \log M_1 + \beta_{12} t + \beta_{13} \log y_1 \\
+ \beta_{14} \log (M_{t-1}/P_{t-1}) + \sum_{i=0}^{3} \beta_{1,6+i} M_{t-i} + \varepsilon_{11}
\]

where \( \varepsilon_{11} \) is the stochastic disturbance. The weight \( T_1 \) measures the importance of direct price linkages relative to domestic conditions in determining the price level, which we term the degree of price linkedness.

The Real Income Equation

The real income equation combines a partial adjustment toward the natural-employment level with the effects of unanticipated innovations in certain stated macroeconomic variables plus those of others represented by a disturbance term.

\[
(3) \quad \log y_1 - \log y_{1t-1} = \psi_{11} + \psi_{12} (\log y^n_{1t-1} - \log y_{1t-1}) \\
+ \text{innovation effects}
\]

The natural-employment real income will not grow steadily because booms and recessions will have lasting effects on the capital stock and hence the level of real income associated with the natural unemployment rate.\(^7\)

\(^7\)Some preliminary calculations and estimates suggest that any adjustment of the capital-labor ratio as predicted by neoclassical growth models proceeds at too slow a pace to be detectible as a movement of natural-employment income toward steady-state income.
The most obvious approach — and the one to be tried first — is to represent natural-employment income by permanent income \( y_1^p \). Logarithmic permanent income is customarily calculated as

\[
(4) \quad \log y_1^p = (1-\theta_1)\psi_{11} + \theta_1 \log y_1 + (1-\theta_1) \log y_{1t-1}
\]

It is not practical to estimate the form which results from applying a Koyck-type transformation to equations (3) and (4) because of numerous nonlinear constraints. So the permanent income approach would require estimating conditional upon a value of \( \theta \) derived from previous research on permanent income and checking that the results are not unacceptably dependent on the particular value of \( \theta \) used.

We wish to include innovation effects for the major macroeconomic shocks which are believed to affect real income: monetary policy, fiscal policy, foreign real income shocks, and unusual strike activity. The first three shocks operate through unexpected growth in aggregate demand for final goods and inventory adjustments. We assume that their maximum effect is achieved within one year and that thereafter any residual effects are eliminated as indicated by the partial adjustment scheme (3). This implies that the nominal money supply does not affect real income in the long run and that there is complete long-run "crowding-out" of real income effects of fiscal policy and foreign real income shocks. We are thus treating as negligible any effects operating via the interest elasticity of money demand on the investment-income ratio and the aggregate production function. The strike variable will be measured as a ratio of man days lost to the civilian labor force. These aggregate supply shocks appear to have a quick effect and recovery which would be completely captured by a one-year distributed lag on their level. We plan to check that the aggregate demand shocks enter as innovations only and not also as anticipated levels.
The combined real income equation to be estimated is

\[
(5) \quad \log y_t = \alpha_{11} + \alpha_{12} \log y^P_{1t-1} + (1-\alpha_{12}) \log y_{1t-1}
+ \sum_{i=0}^{3} \alpha_i,3+i \zeta_{1t-1}^i + \sum_{i=0}^{3} \alpha_i,7+i \zeta_{1t-1}^i + \sum_{i=0}^{3} \alpha_i,11+i \zeta_{1t-1}^i
+ \sum_{i=0}^{3} \alpha_i,15+i \zeta_{1t-1}^i + \varepsilon_{12}
\]

where the fiscal policy innovation is measured as \( \zeta_1 = \log g_1 - (\log g_1)^* \),

the foreign real income shock is \( \zeta_1^R = \log y^R_1 - (\log y^R_1)^* \), and the strike

variable is \( s_1 \).

An alternative approach is to use Okun's law to replace \( \log y^n_{1t-1} - \log y^p_{1t-1} \)
in equation (3) with \( u_{1t-1} - u^n_{1t-1} \). This at first does not appear attractive

because the natural rate of unemployment \( u^n \) is an unknown variable. If,

however, we take first differences of this unemployment version of equation

(3), we obtain

\[
(6) \quad \log y_t = 2 \log y_{1t-1} - \log y_{1t-2} + \alpha_{10} + \alpha_{12} \Delta u_{1t-1} + \Delta(\text{innovation effects})
\]

where movements in \( u^n \) other than trend are lumped into the disturbance.

This explains accelerations in the growth of real income by the lagged change

in the unemployment rate and distributed lags of the changes in the innovations.

A third alternative is to directly model the natural unemployment rate.

The unemployment rate approaches are alternatives for future use because

of the questionable nature and differing meaning of the unemployment data

in many countries in our sample.

The Unemployment Equation

Ideally we would like to determine the unemployment rate as either the

natural rate plus an Okun's Law type adjustment on \( \log (y/y^P) \) or else as the
natural rate plus innovation effects corresponding to the real income innovation effects a la Barro (1977). Either approach requires modeling the natural unemployment rate for each country.

For the present we will assume that the natural unemployment rate has followed a trend if it has changed at all. This means that we can stick with the simple Okun's Law equation.

\[
(7) \quad u_t = \gamma_{11} + \gamma_{12} + \gamma_{13} \log \left( \frac{y_t}{y_t^P} \right) + \epsilon_{13}
\]

An alternative approach similar to that used to derive equation (6) is also of interest. Suppose that the unemployment rate displays a partial adjustment to the lagged difference between the natural and actual unemployment rates and a response to the innovations present in the real income equation.

\[
(8) \quad \Delta u = \lambda_{11} (u_{1t-1}^n - u_{1t-1}) + \text{innovation effects}
\]

If we take first differences in (8) and again relegate changes in the natural rate (aside from trend) to the disturbance term, then

\[
(9) \quad \Delta u_{1t} = \lambda_{10} + (1 - \lambda_{11}) \Delta u_{1t-1} + \Delta(\text{innovation effects}) + \epsilon_{13}^t
\]

So while we plan to try the permanent-income real income and unemployment equations, we have good alternatives as well.

The Interest Rate Equation

We explain the U.S. nominal interest rate by a variable real interest rate version of a Darby (1975) tax-effect modified Fisher equation. That is, the nominal interest rate is the sum of an inflationary premium plus a

\[8\] Barro (1977) allows for no partial adjustment and instead uses long distributed lags on the innovations. A more structured approach is desired here.
real before-tax interest rate:

\[ R_1 = \delta_{11} 4 \cdot [(\log P_{1t+1})^* - \log P_1^*] + \epsilon_1 \]

The coefficient \( \delta_{11} \) of the expected (per annum) inflation rate will exceed unity if the effective marginal tax rate on interest income exceeds the effective capital-gains tax rate on inflationary increases in capital value. We assume that the real interest rate fluctuates around an invariant long-run \( \delta_{10} \) in response to the aggregate demand innovations described in the real income equation (5).\(^9\) So the equation to be estimated is

\[ R_1 = \delta_{10} + \delta_{11} 4[(\log P_{1t+1})^* - \log P_1^*] + \sum_{i=0}^{3} \delta_{1,2+i} \hat{M}_{t-i} + \sum_{i=0}^{3} \delta_{1,6+i} \hat{g}_{1t-i} + \sum_{i=0}^{3} \delta_{1,10+i} \gamma_{1t-i}^R + \epsilon_{14} \]

The standard presumption is that positive money supply innovations temporarily decrease the real interest rate while positive fiscal or foreign-real-income innovations have the opposite effect.

**The Money Supply Reaction Function**

A recurrent problem with reaction function studies is that the goals of policymakers change over time. We assume that these changes are gradual so that they are small in any quarter relative to the perceived changes to which the policymakers respond. This allows us to explain changes in (but not levels of) monetary policy reasonably well on the basis of changes in the policymakers' information set.\(^10\) Considerable empirical investigation of money supply reaction functions has been carried out using this approach as reported by Price (1978).

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\(^9\)Alternative versions of such a tax-effect modified Fisher equation with variable real interest rate are discussed and tested in Carr, Pesando, and Smith (1976).

\(^10\)A formal theoretical development of this approach is contained in Darby (1977a).
Our U.S. fiat money supply reaction function relates accelerations in money supply growth to accelerations in interest rates, inflation, and the unemployment rate.

\[(12) \quad \log M_1 = 2 \log M_{1t-1} - \log M_{1t-2} + \eta_{11} + \eta_{12} (R_1 - 2R_{1t-1} + R_{1t-2}) + \eta_{13} (\log P_{1t-2} - 2 \log P_{1t-3} + \log P_{1t-4}) + \eta_{14} (u_{1t-2} - 2u_{1t-3} + u_{1t-4}) + \xi_{15}\]

The two quarter lags for the inflation and unemployment accelerations are empirical reflections of recognition and inside lags. The Fed's standard operating procedure involves contemporaneous interest rate stabilization, so that term is not lagged. In this regard, our reaction function may be regarded as a semi-reduced form explaining the money supply as determined by the interaction of the banking system and credit policy. We anticipate the need for further empirical experimentation with the lag structure in the context of simultaneous estimation.

**Expected Values**

We have so far used four asterisked variables denoting expected values formed in the previous quarter of the indicated variable. For the most part, these expected values refer to the current or earlier periods and are therefore based on past information. These values are treated as predetermined in estimating the model. The model estimates will be conditional on the particular expectations formation schemes used, however.

Initially we are basing our expected values on univariate time series analysis of each variable following Box and Jenkins (1970). This is not a full
rational expectations approach unless the cost of obtaining or using information in other series is prohibitively costly.\textsuperscript{11} As the model is refined we intend to formulate transfer function estimates of expected values which are based on the own series and on other (lagged) variables which are important in determining the current value. These more elaborately formulated expectations can be used to check the robustness of our conditional estimates of the model.

We are postponing the explicit modeling of $(\log P_{t+1})^*$ and other future expectations required for the other country submodels until the transfer functions have been fitted empirically. We are particularly interested in seeing whether U.S. prices and money supply affect foreign anticipated price levels.

It should be observed that the expected values will generally differ substantially from the predicted value of the corresponding equation in the model. This is because of a difference in timing of information. Consider for example $(\log M_1)^*$ and the money reaction function. The Federal Reserve System bases its behavior — at least in part — on information which comes available within the current period. That information is unavailable at the time expectations are formed. Expectations are formed based on expected values of the variables determining the Fed's monetary policy, but innovations in those variables will contribute to the monetary innovations $\hat{M}_1 = \log M_1 - (\log M_1)^*$.\textsuperscript{12}

\textsuperscript{11}See Darby (1976).

\textsuperscript{12}The stochastic disturbance in the money reaction will also contribute to monetary innovations.
Summary of the U.S. Fiat Submodel

The fiat standard version of the U.S. submodel thus consists of the five equations (2), (5), (7), (11), and (12), identity (4), and a second yet unspecified identity defining \((\log P_{1,t+1})^*\) as a function of current and lagged \(\log P_1\) and other variables. These equations and the variables in the model are displayed in Table 2.

A fiat-reserve-currency country is the implicit standard case for most macroeconomics, so the submodel follows generally familiar lines. Innovations in the nominal money supply, real government spending, and foreign real income have standard short-run effects on real income and the nominal interest rate. The price level adjusts to equate nominal money demand to the anticipated nominal supply, with allowance for possible effects of foreign price shocks. The endogenous nominal money supply -- surprising to some in a "monetarist" model -- evolves over time in response to the effects on interest rates of innovations in fiscal policy and foreign real income as well as the evolution of inflation and unemployment and other shocks.

Gold Standard Amendments to the U.S. Submodel

This version of the U.S. submodel is proposed to test empirically whether the U.S. was in fact on the gold standard during the early part of our sample period. It is an empirical question since it depends on whether or not the Fed adjusted the money supply in response to changes in the gold stock. If not, the fixed exchange rate of gold for dollars amounted to no more than a price support program without substantial economic implications.

There are two alternative explanations for the acceleration of U.S. money supply growth in the 1960's and the consequent worldwide inflation:

1. The removal of gold reserve requirements on Federal Reserve notes and deposits may have freed the Fed from a powerful restraining force. Afterward
it was free to pursue more rapid monetary growth than it would otherwise have chosen. (2) The Fed paid no attention to the gold stock anyway.

The accelerated growth of the nominal money supply was in response to the pressure on the interest rate of accelerating deficits to finance the Vietnamese War. It is not, therefore, indicative of future accelerating inflation absent such extraordinary fiscal shocks.

If the U.S. were de facto on a gold standard in the early part of our period, the gold stock would enter the money reaction function. Some experimentalism with lags and form will be necessary, but let us suppose for the current exposition that we add to our money reaction function the change in the change in the gold stock $B_{1}$. Our alternative money reaction function would be

\[(12') \log M_{1} = 2 \log M_{1t-1} - \log M_{1t-2} + \eta_{11} + \eta_{12}(R_{1t-2}R_{1t-1} + R_{1t-2})
+ \eta_{13}(\log P_{1t-2} - 2 \log P_{1t-3} + \log P_{1t-4})
+ \eta_{14}(u_{1t-2} - 2u_{1t-3} + u_{1t-4})
+ \eta_{15}(B_{1t-2} - B_{1t-3}) + \varepsilon_{15}\]

While the U.S. stood ready to exchange gold at $35 per ounce, it was the residual supplier or demander of gold. The change in the U.S. gold stock equalled the excess supply of gold taking account of all other international supplies and demands. The excess supply of gold is an increasing function of the price of gold relative to the equilibrium price of gold. The price of gold in terms of goods is the inverse of the price level, so the price ratio referred to is $P_{0}^{eq}/P_{1}$. A linear version of the required excess demand function is
(13) \[ B_1 = \xi_{11} + \xi_{12} \log \frac{p_{1eq}}{p_1} \]

Suppose that the equilibrium price level \( p_{1eq} \) follows a martingale with drift in the logarithms

(14) \[ \log p_{1eq} = \log p_{1eq}^{\text{lt-1}} + \xi_{13} + \gamma_t \]

Taking first differences in equations (13), (14), substituting, and simplifying the notation

(15) \[ B_1 = B_{1t-1} + \rho_{11} + \rho_{12} (\log p_1 - \log p_{1t-1}) + \epsilon_{16} \]

If the gold standard version (12') of the money reaction function proves empirically interesting, we will proceed further with specification of the gold stock change equation.
II. Nonreserve Country Submodels

All of the country submodels other than the United States have the same form. We anticipate future modifications — particularly in the money supply reaction functions — to tailor these models to national institutional arrangements, but that has not been done yet. We present in this section the prototypical model for country \( j \) (\( j = 2, 3, \ldots, 8 \)), taking foreign variables as exogenous. As with the U.S., the endogeneity of the foreign variables will be introduced in Section III.

Overview

The real income, price level, and unemployment rate equations are the same as in the U.S. submodel. These equations are of quite general form and can accommodate national differences — such as in price linkedness \( T_j \) — by different parameter values. The nominal interest rate equation is generalized to allow for interest arbitrage linkages. The money supply reaction function — as in the gold standard version of the U.S. submodel— allows for possible influences of the balance of payments. The balance of payments is determined by a generalization of the standard monetary approach equation under pegged exchange rates. This generalization allows for substitution effects due to changes in the purchasing power ratio as well as the familiar liquidity effects due to excess money demand. Under floating exchange rates the dual equation allows for possible transitory effects on the purchasing power ratio from excess money demand and government intervention in the foreign exchange market. Such government intervention is determined by a stabilization function.

\[ \text{This influence is necessary but not sufficient both for the specie-flow mechanism and for monetary adjustment under complete price linkedness (} T_j = 1). \]
The Price Level Equation

The price level equation is of the same form as the U.S. equation (2):

\[
\log P_j = \beta_{j1} + T_j (\log P_j^R + \log E_j) + (1-T_j) \log \Pi_j + \beta_{j2} t \\
+ \beta_{j3} \log y_j + \beta_{j4} R_4 + \beta_{j5} \log (\hat{M}_{jt-1}/P_{jt-1}) + \sum_{i=0}^{3} \beta_{j6+i} \hat{I}_{jt-1} + \epsilon_{j1}
\]

Here the coefficient of price linkedness \( T_j \) provides a ready measure of the importance of direct price linkages, so much emphasized by the "global monetarists."\(^{14}\) If this coefficient is small, then the effect of the balance of payments on the money supply would be the main channel by which long-run purchasing power parity at a fixed exchange rate could be achieved.

The Real Income Equation

The real income equation applicable to the U.S. holds generally, so

\[
\log y_j = \alpha_{j1} + \alpha_{j2} \log y_{j,t-1}^P + (1-\alpha_{j2}) \log y_j + \sum_{i=0}^{3} \alpha_{j,3+i} \hat{I}_{jt-1} \\
+ \sum_{i=0}^{3} \alpha_{j,7+i} \hat{R}_{jt-1} + \sum_{i=0}^{3} \alpha_{j,11+i} \hat{y}_{jt-1} + \sum_{i=0}^{3} \alpha_{j,15+i} \hat{s}_{jt-1} + \epsilon_{j2}
\]

This approach also requires the definitional identity for permanent income

\[
\log y_j^P = (1-\theta_j) \psi_{j1} + \theta_j \log y_j + (1-\theta_j) \log y_j^P
\]

As with the U.S., we plan to consider an alternative unemployment-rate approach to real income determination. It is generally supposed that foreign real income shocks will be relatively more important for the smaller countries

\(^{14}\) See Whitman (1975). Note that \( P_j^R \) is an index of foreign prices converted into dollars per unit of output. Therefore the product \( P_j^R E \) is in terms of \( j \) currency per unit of output. Details of the calculation are in Section III.
in our sample. We can check this hypothesis by examining the coefficients \( a_{j,11}, \ldots, a_{j,16} \).

**The Unemployment Equation**

As with the U.S. submodel, we posit a simple Okun's Law relation

\[
(19) \quad u_j = \gamma_{j1} + \gamma_{j2} t + \gamma_{j3} \log \left( \frac{y_j}{y_j^P} \right) + \epsilon_{j3}
\]

There is an alternative approach to be tried relating the change in the unemployment rate to the lagged change and changes in the innovations.

**Balance of Payments: Pegged Exchange Rates Case**

The discussion that follows is simplified by defining the logarithm of the purchasing power ratio as

\[
(20) \quad Q_j \equiv \log P_j^R + \log E_j - \log P_j
\]

Since \( \log P_j^R \) and \( \log P_j \) are determined elsewhere in the model, determination of \( Q_j \) is equivalent to determining the logarithm of the exchange rate, \( \log E_j \).

In the monetary approach to the balance of payments and exchange rates, it is generally assumed that \( Q_j \) is always at its parity value because of commodity arbitrage (the law of one price level). The balance of payments is related to the difference between the nominal demand for (high-powered) money and the nominal supply of (high-powered) money from sources other than central bank foreign exchange operations. The logic of a depreciation of the exchange rate is that it increases the domestic price level, which increases nominal demand for high-powered money, which causes reserves to flow in until the gap is filled. There is no role here for the specie-flow mechanism in which changes in \( Q_j \) cause reserve flows by making tradable-goods consumption less attractive and their production more attractive.
So to consider the possibility that inflation is transmitted through the specie-flow mechanism, we must generalize the monetary approach.

Let us first consider the case of pegged exchange rates. In that case we take exchange rates as exogenous. The balance of payments, as is customary in the monetary approach, is scaled by taking it as a ratio to high-powered money, or \( B_j/H_j \). The scaled balance of payments is supposed normally to be some fraction of the logarithmic change in high-powered money. This amount will be increased if monetary policy is used to create an excess demand for money for the standard monetary approach reasons. It will also be increased if the purchasing power ratio \( Q_j \) exceeds its parity value.

A combined balance of payments equation would be

\[
\frac{B_j}{H_j} = \nu_{j0} + \nu_{j1} (\log H_j - \log H_j, t-1) + \nu_{j2} Q_j + \nu_{j3} (\log M_j - \log P_j) + \nu_{j4} r + \nu_{j5} \log y_j + \nu_{j6} r_j + \sum_{i=0}^{3} \nu_{j7+i} R_j, t-1 + \epsilon_{j6}
\]

This equation is derived on the assumption that the parity value of \( Q_j \) follows a trend which can be incorporated in \( \nu_{j0} \) and \( \nu_{j4} \). The influence of the real supply of money relative to its real demand is measured by \( \nu_{j0} \) and \( \nu_{j3}, \nu_{j4}, \ldots \nu_{j10} \). A significantly positive coefficient \( \nu_{j2} \) indicates relative price level changes do have a role in explaining the balance of payments as required for the specie-flow adjustment process. Since the parity value of \( Q_j \) may well follow a martingale with drift.

---

15 Note that \( B_j = \nu_{j1} (H_j - H_j, t-1) \) implies \( B_j/H_j = \nu_{j1} (\log H_j - \log H_j, t-1) \).

16 This model is similar to that discussed in a no-growth context by Connolly and Taylor (1976). However the variations in relative prices there were between tradable and nontradable goods.

17 That is, if \( \bar{Q}_j \) is the parity value, it may be that \( \bar{Q}_j = \bar{a} + \nu_{j1} r_{j1} + \nu_j \), where the \( \nu_j \)'s are uncorrelated random variables. This would be consistent with changes in \( \bar{Q}_j \) over time because of relative price changes for individual exports and imports. See Stockman (1978) for evidence that \( \bar{Q}_j \) is nonstationary.
the first difference form of equation (21) will be tried also.

Since the balance of payments is related, following the monetary approach, to the change in the reserve component of high-powered money, we must use the money multiplier \( \mu \); to move from the money supply (determined by the money supply reaction function) to high-powered money. We take the money multiplier \( \mu \) as exogenously determined so that (the logarithm of) high-powered money is defined by the identity

\begin{equation}
(22) \quad \log H_j = \log M_j - \log \mu_j
\end{equation}

Exchange Rates and Balance of Payments: Floating Exchange Rate Case

Under floating exchange rates, the monetary approach would suggest that the exchange rate will adjust to equate \( Q_j \) with its parity value given \( \log P_j^R \) and \( \log P_j \). If we are to allow \( Q_j \) to differ from parity in the pegged rate case, we must admit a corresponding possibility in the floating case, particularly with regard to government "exchange-rate stabilization" operations.

Writers in the monetary approach literature would argue that it would make no difference to the guilder/dollar exchange rate, say, whether the Dutch central bank achieved a given nominal money supply by purchasing U.S. treasury bills or Netherlands treasury bills. We suppose that these assets might not perfect substitutes so that there would be different net capital flows -- and relative yields -- in the two cases. \(^{18}\) These different net capital flows would imply different net exports and values of \( Q_j \) if the law of one price level does not hold.

\(^{18}\) Milton Friedman suggested that a useful analogy would be to consider whether it would affect the price of real estate if the Fed bought real estate instead of U.S. treasury bills to achieve a given increase in the money supply. Whether the effects are sufficiently small and transient to be negligible is an empirical, not theoretical, question.
The dual of equation (21) which we propose to estimate under floating exchange rates is

\[(21') \quad Q_j = z_{j0} + z_{j1} (\log H_j - \log H_j, t-1) + z_{j2} \frac{B_j}{H_j} + z_{j3} (\log H_j - \log P_j) + z_{j4} t + z_{j5} \log y_j + z_{j6} R_j + \sum_{i=0}^{3} z_{j,7+i} M_j, t-i + \epsilon_{j6} \]

If the law of one price level and perfect asset substitution are acceptable empirical approximations, only factors determining the parity value of \(Q_j\) — here the constant and time — will enter.\(^{19}\) Here we allow for the possibility of short-run effects on the parity ratio from exchange-market intervention and monetary policy effects on real interest rates.

If we were dealing with clean floats, \(B_j/H_j\) would be exogenously set independently of the exchange rate.\(^{20}\) In the dirty floats which we have observed, there appears to be an attempt to stabilize the exchange rate. So we assume that \(B_j/H_j\) is determined by a policy reaction function as a distributed lag of current and past exchange rate changes:

\[(23) \quad \frac{B_j}{H_j} = c_{j1} + \sum_{i=0}^{3} c_{j,2+i} (\log E_j, t-i - \log E_j, t-i-1) + \epsilon_{j7} \]

**Money Supply Reaction Function**

Movement to equilibrium under pegged exchange rates requires that an increased balance of payments surplus lead to increased monetary growth.

\(^{19}\) Then the equation would reduce to the standard monetary approach equation (after first-differencing): \(\Delta \log E_j = a + \Delta \log P_j - \Delta \log P_j^R + \nu.\)

\(^{20}\) This would not necessarily be zero since the Netherlands might wish to invest transitory natural gas revenues in U.S. treasury bills for portfolio reasons.
This is true whether one emphasizes direct price linkages or specie-flows as the adjustment mechanism. \(^{21}\) Thus the reserve currency reaction function would be supplemented by a term in the change of the scaled balance of payments.

Preliminary experimentation reported in Price (1978) suggests that the scaled balance of payments should be lagged several quarters. This is consistent with the standard central bank practice of automatically sterilizing via open market operations the money supply effects of foreign exchange operations.

Under pegged exchange rates the money supply reaction function would be similar to that of the reserve currency under the gold standard:

\[
\log M_j = 2 \log M_{jt-1} - \log M_{jt-2} + \eta_{j1} + \eta_{j2} (R_j - 2R_{jt-1} + R_{jt-2}) \\
+ \eta_{j3} (\log P_{jt-2} - 2 \log P_{jt-3} + \log P_{jt-4}) \\
+ \eta_{j4} (u_{jt-2} - 2u_{jt-3} - u_{jt-4}) \\
+ \eta_{j5} \left[ \frac{B_j}{H_j t-2} - \frac{B_j}{H_j t-3} \right] + \epsilon_{j5}
\]

The floating rate version would drop the \( \eta_{j5} \) term, although we intend to test whether this is in fact the case.

The Interest Rate Equation

As with the price equation, we wish to allow the data to determine the relative importance of domestic forces and international forces (interest

\(^{21}\) It may be that pegged exchange rates are periodically adjusted instead of monetary growth. Unfortunately it is empirically impossible to estimate a reaction function for the infrequent exchange rate changes so we treat them as exogenous shocks.
arbitrage) in determining the nominal interest rate. Strict interest arbitrage would relate the nominal interest rate to the U.S. nominal interest rate and the expected growth rate per annum of the exchange rate. We add a term in the scaled balance of payments to allow for variations in the risk premium. Adding these to the domestic variables in the U.S. equation (11) yields

\[
R_j = \delta_{j0} + \delta_{j1} 4[\log P_{jt+1}^* - \log P_j] \\
+ \sum_{i=0}^{3} \delta_{j,2+i} \hat{M}_{jt-i} + \sum_{i=0}^{3} \delta_{j,6+i} \hat{x}_{jt-i} + \sum_{i=0}^{3} \delta_{j,10+i} \hat{\gamma}_{jt-i} \\
+ \delta_{j,14} R_j + \delta_{j,15} 4[\log E_{jt+1}^* - \log E_j] \\
+ \delta_{j,16} \frac{B_i}{H_j} + \varepsilon_{j4}
\]

**Summary of the Standard Nonreserve Country Submodel: Pegged Exchange Rate Version**

The pegged exchange rate version of the nonreserve country submodel is presented in Table 3, which includes the yet unspecified identities for expected future values. The major difference from the U.S. fiat submodel is the potential importance of the scaled balance of payments in determining the money supply. There is also an interest rate linkage and direct price linkage which would probably be more important than in the U.S. case.

The nonreserve country money stock will evolve over time in response to domestic shocks and the balance of payments. If the degree of price linkedness is high, U.S. inflation would be transmitted directly, with the nominal money supply then rising to make up for the inflation-induced fall in the real money supply. Our model alternatively permits the purchasing power ratio to get out of line (if price linkedness were low) so that the
balance of payments is increased via "expenditure-switching" and consequent changes in absorption. This causes money and prices to rise over time until the purchasing power ratio falls to its parity value.

Changes for the Floating Exchange Rate Version

The minor changes required for the floating exchange rate version of the nonreserve country submodel are presented in Table 4. If the addition of equation (23) is spurious in the sense that the balance of payments is an exogenous variable (say 0) due to nonintervention, then the model is identical to the U.S. fiat submodel except that we happen to normalize on the U.S. exchange rate and include the exchange rate equations here. We choose to allow for the possibility of these countries having temporary effects on the purchasing power ratio via intervention so that the data can decide the issue.
III. International Connections: Closing the Model

We close the model by making endogenous the previously predetermined current foreign variables and combining the submodels. Nothing is required for the U.S. interest rate $R_1$ since it is already defined as endogenous in the U.S. submodel. However, all eight submodels have foreign real income and price variables ($\log y^R_j$ and $\log P^R_j$) which must be defined. This is done by sixteen identities.

The Foreign Real Income Identities

The operational measure of foreign real income for each country $j$ ($j = 1, \ldots, 8$) is a nominal-income-weighted index of the real income of the other seven countries. Our nominal-income weights are based on averages for the entire sample period. First, the overall nominal income weight $V_j$ is calculated for each country. This is done by converting nominal income $Y_j$ into dollar equivalents via exchange rates and then calculating mean nominal income $\bar{Y}_j$ for the country over the sample period. The share of each country in total mean nominal income is

\begin{equation}
V_j = \frac{\bar{Y}_j}{\sum_{i=1}^{8} \bar{Y}_i}
\end{equation}

The overall weight $V_j$ is the share of country $j$ in total mean nominal income. For computing country $j$'s foreign real income, we want the weight of country $i$ in the total mean nominal income of all countries other than $j$. This is

\begin{equation}
d_{ji} = \frac{V_i}{1-V_j} \quad \text{for } i, j = 1, \ldots, 8; i \neq j
\end{equation}
These computed nominal income weights are used in our foreign real income identities

\[ \log y_j^R = \sum_{i=1}^{8} d_{ji} \log y_i^1 - \text{base}_{y_j}, \quad j = 1, \ldots, 8 \]

where \( \text{base}_{y_j} \) is the number that makes \( \log y_j^R \) average 0 over the base year. This index is algebraically equivalent to one which computes the growth rate of foreign real income as the weighted (by \( d_{ji} \)) sum of the individual foreign real income growth rates.

The Foreign Price Identity

The foreign price variable is an index of foreign prices converted by the exchange rates into dollars per unit of real output. In terms of levels, we divide country \( i \)'s price index \( P_i \) (in \( i \) currency per unit of output) by its exchange rate \( E_i \) (in \( i \) currency per dollar) to obtain the price in dollars of a unit of output in \( i \). Taking the weighted average over all foreign countries of the \( \log (P_i/E_i) \) gives our foreign price identities.

\[ \log P_j^R = \sum_{i=1}^{8} d_{ji} (\log P_i - \log E_i) - \text{base}_{P_j}, \quad j = 1, \ldots, 8 \]

where \( \text{base}_{P_j} \) normalizes \( \log P_j^R \) to zero in 1970.

Note that \( \log P_j^R + \log E_j \) is the logarithm of a similar index computed using the implicit exchange rate \( E_i/E_j \) of \( i \) currency per unit of \( j \) currency.\[22\] This corresponds to an index \( y_j^R = e^{\log y_j^R} \) which equals 1.000 in 1970.
This index $P^E_j$ is the weighted average cost in $j$ currency of a unit of output abroad.

The sixteen identities (28) and (29) complete the model by making foreign real income and prices endogenous.

**International Transmission in the Mark II Model**

There have been proposed in the literature a large number of channels by which inflation can be transmitted internationally. The Mark II model represents substantial progress toward empirical measurement of the importance of these various channels.

Let us first consider the channels which existed under the pegged exchange rate system. The extent to which prices are determined via commodity arbitrage (the law of one price level) is measured by $T_j$, the coefficient of price linkedness. If $T_j$ is near 1, as assumed in much of the monetary approach literature, then country $j$'s price level will adapt quickly to the world price level with the nominal money supply passively adjusting to changes in nominal money demand caused by world price level changes. The speed with which the money supply adjusts would depend on the effect of excess money demand on the scaled balance of payments and the effect of the scaled balance of payments on the nominal money supply.

If price linkedness is low, the world price level will not follow U.S. price developments so closely. In particular an acceleration in U.S. inflation would have little initial effect on the foreign country $j$'s price level but would instead increase the purchasing power ratio. This would induce expenditure-switching increases in the scaled balance of payments which would in turn lead to increases in the money supply. As the money supply increases begin to affect country $j$'s price level, the purchasing
power ratio will finally begin to fall. This process involves a catch-up period of very rapid money and price growth and finally a permanent increase in these growth rates by the amount of the permanent increase in U.S. inflation.  

Interest rate and real income linkages are also included. We anticipate that the most important effects of these linkages will operate through induced changes in the nominal money supply. We have not yet provided for external shocks such as OPEC and the famous Peruvian anchovies. The reason is that the model has the potential to explain the worldwide price explosion of the early 1970s without such *dei ex machinae* and we would like to see empirically how much remains to be attributed to such shocks. Given their unique nature any direct inclusion in the model at this point might well beg the question.

Under flexible exchange rates, each country's inflation rate is substantially determined by its own domestic considerations. It may be that its domestic monetary policy is influenced by the effects of foreign shocks. An interesting question is whether government intervention in foreign exchange markets has had a substantial effect on exchange rates. Such an effect would be the dual of the ability of a government to exercise short-run control of its nominal money supply under exchange rates via sterilization.

We hope to discover whether the accelerated U.S. nominal money supply growth in the decade centered around 1970 can be attributed to abandonment of the gold standard or to printing money to finance the Vietnamese War. The answer to this question will be useful in assessing prospects for U.S. inflation under present and alternative monetary arrangements.

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23 The dynamic analysis of such a system is quite complicated. It will be discussed in a forthcoming paper by Dean Taylor and the author.
IV. Estimation Methods

The standard two-stage least squares estimator does not exist for the Mark II model because the number of predetermined variables (instruments) exceeds the number of observations. It will be recalled that the first stage consists of obtaining fitted values of the endogenous variables from their reduced-form regression on all the instruments. The second stage is an equation-by-equation OLS estimation of each structural equation with the actual values of the endogenous variables replaced by their fitted values. If the instruments are truly exogenous, they will be independent of the disturbances in the structural equations and so too, the argument goes, will be the fitted values of the endogenous variables. It is this independence of the fitted values from the disturbances which removes the problem of simultaneous equation bias.

Unfortunately the consistency of the 2SLS estimator depends crucially on the number of observations going to infinity while the number of instruments is fixed. Each instrument can be thought of as explaining the structural disturbances for one observation. In the extreme where the number of instruments equals (or exceeds) the number of observations, the fitted values will exactly equal the actual values for the endogenous variables so that 2SLS and OLS are identical and no simultaneous equation bias is removed.

If we wish to reduce simultaneous equation bias, we must restrict our list of instruments to a number less than the number of observations. This involves a tradeoff of less efficiency for less bias which has not been analyzed in the literature. To the extent that the question has been considered at all; judgment appears to be the only guide as to how many and which instruments to use. We plan to examine this issue rigorously in the future and to perform a sensitivity analysis with the final form of the model to determine how our 2SLS estimates converge to OLS estimates as we
lengthen our list of instruments.

We have chosen to follow a country-by-country procedure for selecting instrument lists. The first step is to form a basic instrument list for each country consisting of the domestic exogenous and other predetermined variables appearing in the submodel for that country. This basic list is used to obtain fitted values for real income, the price level, and (for the U.S. only) the nominal interest rate. These fitted values are then used as if exogenous wherever they appear as foreign variables in the submodels for other countries. Then each submodel was estimated separately based on an instrument list consisting of the domestic instruments and the fitted rest-of-world variables. Thus each submodel is estimated with an instrument list which has a number of variables less than half the number of observations.

For each country this augmented instrument list resulted in a non-invertible cross-products matrix. We have used the principal components option in the TROLL system to obtain the approximately 20 principal components which explain 100.0 percent of the generalized variance in the instrument list. Having thus extracted virtually all the information in the instrument list, we then carry out 2SLS using these principle components as the right-hand variables (instruments) in estimating the fitted values of the country's endogenous variables in the first stage.

It may be noted that in obtaining the fitted rest-of-world variables

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24 Because of lagged values and identities, certain of the basic instruments had to be deleted in order to obtain a list with a cross-product matrix which the computer could invert. Table 5 divides the basic instrument list for each country into those which were used to estimate these fitted values and those which were excluded. Some other variables were not even included in the basic instrument list because they were by definition linear combinations of included variables.
(instead of using principal components) we judgmentally deleted variables showing high simple correlation with included variables to obtain an invertible cross-products matrix. This was done because the TROLL package does not permit recovery of first-stage fitted values based on the principal components option. In the current case where both methods essentially span the instrument list, it probably makes no difference which procedure is used. When we reduce the number of instruments to conduct the sensitivity analysis discussed previously, the results will be different in view of the non-invariance of principal components to linear transformations. This is another interesting econometric issue to be explored further.
V. Estimation Results

First-pass estimates of the fixed-exchange-rate Mark II model were made for the entire period 1957-I to 1976-IV. This was the longest available taking account of the required lagged values of some variables. We do not believe that all of the equations were invariant with respect to introduction of free convertibility (generally in 1958) and floating exchange rates (generally during 1971-1973). Nevertheless, we thought it useful to have a set of estimates for the entire period with which alternative subperiod could be compared.

Our results are presented here on an equation-by-equation basis. Money stock definitions depend on which concept appears most consistent with the country's economic institutions as judged by the real income, price level, and reaction function equations (see Table 6).

Price Level Equations

The price level equations\(^{25}\) are generally very good in terms of standard errors, \(R^2\)'s, and Durbin-Watson statistics as seen in Table 7. The coefficients are generally as predicted by theory, except that the estimated coefficients of price linkedness are all near zero. There are arguments which suggest that this coefficient would be biased toward zero. In response to insightful comments from Guy Stevens, we plan to remove the foreign price level variable from the price level equations and move it to the balance of payments sector as discussed below. This makes the price level equation simply the equality of (short-run) demand for and supply of money. The revised equations are presented in Table 7A.

\(^{25}\) Equations (2) and (16) above.
Real Income Equations

The estimated real income equations reported in Table 8 presented some surprises. Basically, these were (1) the relatively small t-statistics on money innovations for most countries other than the United States and (2) the extremely large estimated coefficients of foreign-real-income innovations.

The small money-innovation t-statistics might be due to: (1) the impotence of monetary shocks, (2) the passivity of monetary policy, particularly under fixed exchange rates, (3) errors-in-the-variables due to our construction of the expected log M series, and (4) measurement errors generally. We tested for the third possibility by adding anticipated money to the equation, and concluded that there is some problem with our estimated log M* series for Canada and Japan, but not elsewhere. We will work further on this once the reaction functions are settled. We hope to differentiate between impotence and passivity of monetary policy by contrasting the fixed and floating rate periods as to estimated coefficients and size of innovations, but that work is still in its early stages. Measurement errors are a generally confounding problem for a considerable portion of our countries.

The more serious surprise was the very high foreign-real-income-innovation coefficients. If they were true, this would indicate some channel of influence other than the traditional export demand must be operative. However, we believe that the coefficients reflect correlation among real-income residuals across countries which was not removed by our estimation method. First, Table 8A shows that using real export innovations \( x \) instead of their proxies \( y^R \) results in reasonable coefficients. Secondly, Table 8B shows that ending the period at 1971 II eliminates substantial summed \( y^R \) coefficients for all

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Equations (5) and (17) above.
countries except the United States, Canada, and Netherlands. The period after 1971 II was characterized by widespread price controls which would introduce correlated measurement errors in the deflated instruments and real income. Therefore using fitted real income will not eliminate simultaneous equation bias of this sort. Further, the creation of OPEC may introduce further correlation in the residuals not eliminated by the instruments. Since the problem does appear to be simultaneity bias, we plan to switch to an exports innovation term in the Mark III model with exports explained in the revised balance of payments sector.

We have not yet been able to obtain data on the strike variable for most of our countries. We have therefore excluded it from estimations of the real income equation to date. We currently plan to include it in the Mark III on a where-available basis.
Unemployment Equations

The estimated unemployment equations are presented in Table 9. The Durbin-Watson statistics were unacceptably low. The autocorrelated residuals reflected rather gradual movements in the apparent natural rate of unemployment. Besides demographic factors, these may well reflect unreported changes in the effective definition of unemployment reflected in these data. A revised unemployment rate equation relating the change in the unemployment rate to current and lagged logarithmic changes in real income is presented in Table 9A. This performs well for the United States and passably for the United Kingdom, Canada, and France. For the rest, changes in the unemployment rate appear uncorrelated with past and present changes in real output. This will be explored further, but it may well reflect the tenuousness of the defined unemployment data.

27Equations (5) and (19) above.
Money Supply Reaction Functions

The money supply reaction functions reported in Table 10 display a spurious accuracy. The standard errors do not always compare well to the standard deviation of the change in the growth rate.

Considerable work has been done here which indicates that the reaction functions must be tailored to the individual country's institutions. For example, Germany and Japan show much more substantial and immediate money supply responses to balance of payments surpluses than is the norm. We have found that the current change in the scaled balance of payments enters the reaction function for many nonreserve-currency countries and we are planning to include it as well as lagged changes. \(^29\) Also the moving average error process derived in Darby (1977a) and elaborated in John Price's thesis is found to be important for most of the countries. For some countries where the unemployment data is suspect, we are experimenting with the growth rate of real income in lieu of the change in the unemployment rate. We also plan to try U.S. monetary accelerations for the nonreserve countries. The interest rate coefficient apparently reflected the liquidity effect; so following Barro (1977) we have substituted innovations in real government spending as an alternative measure of fiscal pressure. It appears that these changes will provide acceptable reaction functions for our countries, although the United Kingdom may be little improved relative to a random walk in the money supply growth rate.

\(^{28}\) Equations (12) and (24) above.

\(^{29}\) Note however that the current effect is always in the range of 0.2 or less indicating nearly complete initial sterilization.
Interest Rate and Balance of Payments Equations

The interest rate equations\textsuperscript{30} and the balance of payments equations\textsuperscript{31} are reported in Tables 11 and 12 respectively. We are dissatisfied with them and have adopted a new approach for the Mark III. This new approach is the subject of the next section.

\textsuperscript{30} Equations (11) and (25) above.

\textsuperscript{31} Equation (21) above.
VI. Moving to the Mark III Model

The specification of price-level, balance-of-payments, and interest-rate equations in the Mark II model has proved to be inadequate. Primarily, this is due to the empirical weakness of the monetary approach to the balance of payments (MABP). The nearly complete current quarter sterilization and barely detectible direct influence of foreign prices on domestic prices means that the price equation de facto sets money supply and money demand equal and that there is no excess money demand to be reflected in balance-of-payments surpluses.

The apparent strength of MABP in previous empirical work seems to this author to reflect nothing more than a spurious explanatory power due to the fallacious assumption that "domestic credit" is exogenous. If total money is what the central bank determines (either directly or via pegged interest rates) with domestic credit variations reflecting sterilization of the balance of payments, treating domestic credit as exogenous will give a very good explanation of the balance of payments when combined with the demand for money.

We propose to reformulate these equations in the Mark III so as to be less sensitive to near zero values of the MABP parameters. As already noted, the "price equation" will now simply require equality of money demand and supply. The interest rate equation will be based on aggregate demand equilibrium. The balance of payments will be broken into separate import, export, and capital flow equations with the balance of payments identity requiring asset market equilibrium. The strict MABP results would still be possible if capital and trade flows proved sufficiently

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responsive to deviations from covered-interest and purchasing power parities. In that case the money supply would adjust via the effect of the current balance of payments in the reaction function. But a lagged specie-flow type adjustment would also be possible. Preliminary work along these lines is encouraging.

It is appropriate to conclude with a word of caution that the encouraging results to date do not necessarily portend future success. Since we find it very hard to conceal our undue optimism and enthusiasm, it is hoped that a sincere request for suggestions for further improvements and tests will suffice.
REFERENCES


Table 1
Symbols Used in Mark II Model

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$B_j$</td>
<td>Balance of payments measured in billions of domestic currency units (DCUs) per annum. (For nonreserve countries this is the official reserve settlement basis. For the U.S., we will try changes in the gold stock and the official reserve settlement basis.)</td>
</tr>
<tr>
<td>$E_j$</td>
<td>Exchange rate in DCUs per U.S. dollar ($E_1 = 1$).</td>
</tr>
<tr>
<td>$g_j$</td>
<td>Fiscal policy variable. (We plan to try both NIA real government spending and deficit.)</td>
</tr>
<tr>
<td>$H_j$</td>
<td>High-powered (or base) money in billions of DCUs.</td>
</tr>
<tr>
<td>$M_j$</td>
<td>Money stock in billions of DCUs. (We will try both $M_1$ and $M_2$ definitions to see which best fits the country's institutional framework.)</td>
</tr>
<tr>
<td>$P_j$</td>
<td>Price deflator for GNP (or GDP) in DCUs per base-year DCU. (1970 = 1.000)</td>
</tr>
<tr>
<td>$P_j^R$</td>
<td>Index of foreign prices converted by exchange rates into U.S. dollars per base-year U.S. dollar.</td>
</tr>
<tr>
<td>$Q_j$</td>
<td>Purchasing power ratio ($E_jP_j^R/P_j$) in base-year DCUs per base-year U.S. dollar.</td>
</tr>
<tr>
<td>$R_j$</td>
<td>Short-term nominal interest rate in decimal per annum form. (Three-months treasury bill yield where available.)</td>
</tr>
<tr>
<td>$s_j$</td>
<td>Strike variable. (Man days lost per annum divided by civilian labor force where available.)</td>
</tr>
<tr>
<td>$t$</td>
<td>Time index (1955 I = 1, 1955 II = 2, etc.)</td>
</tr>
<tr>
<td>$u_j$</td>
<td>Unemployment rate in decimal form.</td>
</tr>
<tr>
<td>$y_j$</td>
<td>Real GNP (or GDP if GNP unavailable) in billions of base-year DCUs.</td>
</tr>
</tbody>
</table>
$y_j^p$ Permanent income in billions of base-year DCUs.

$y_j^r$ Index of foreign real income. (1970 = 1.000)

$\mu_j$ Money multiplier ($\mu_j \equiv M_j / H_j$).
Table 2

Fiat Standard Version of U.S. Submodel

Equations

\[
(2) \quad \log P_1 = \beta_{11} + T_1 \log P_1^R + (1-T_1) \log M_1 + \beta_{12} \log y_1 + \beta_{13} \log y_1 \\
\quad \quad \quad \quad + \beta_{14} R_1 + \beta_{15} \log \left( M_{1t-1}/P_{1t-1} \right) + \sum_{i=0}^{3} \beta_{1,6+i} \hat{H}_{1t-1} + \varepsilon_{11}
\]

\[
(5) \quad \log y_1 = \alpha_{11} + \alpha_{12} \log y_{1t-1}^P + (1-\alpha_{12}) \log y_{1t-1} \\
\quad \quad \quad \quad + \sum_{i=0}^{3} \alpha_{1,3+i} \hat{H}_{1t-1} + \sum_{i=0}^{3} \alpha_{1,7+i} \hat{E}_{1t-1} + \sum_{i=0}^{3} \alpha_{1,11+i} \hat{y}_{1t-1} \\
\quad \quad \quad \quad + \sum_{i=0}^{3} \alpha_{1,15+i} \hat{s}_{1t-1} + \varepsilon_{12}
\]

\[
(7) \quad u_1 = \gamma_{11} + \gamma_{12} \log \left( y_1/y_1^P \right) + \varepsilon_{13}
\]

\[
(11) \quad R_1 = \delta_{10} + \delta_{11} 4 \left[ (\log P_{1t+1})^* - \log P_1 \right] \\
\quad \quad \quad \quad + \sum_{i=0}^{3} \delta_{1,2+i} \hat{H}_{1t-1} + \sum_{i=0}^{3} \delta_{1,6+i} \hat{E}_{1t-1} + \sum_{i=0}^{3} \delta_{1,10+i} \hat{y}_{1t-1} + \varepsilon_{14}
\]

\[
(12) \quad \log M_1 = 2 \log M_{1t-1} - \log M_{1t-2} + \eta_{11} + \eta_{12} \left( R_1 - 2R_{1t-1} + R_{1t-2} \right) \\
\quad \quad \quad \quad + \eta_{13} \left( \log P_{1t-2} - 2 \log P_{1t-3} + \log P_{1t-4} \right) \\
\quad \quad \quad \quad + \eta_{14} \left( u_{1t-2} - 2u_{1t-3} + u_{1t-4} \right) + \varepsilon_{15}
\]

Identities

\[
(4) \quad \log y_1^P = (1-\theta_1)\psi_{11} + \theta_1 \log y_1 + (1-\theta_1) \log y_{1t-1}^P
\]
\(-\) \( (\log P_{1,t+1}^*) = f(\log P_{1}, \log P_{1,t-1}, \ldots) \)

**ENDOGENOUS VARIABLES**

\(\log P_{1}, \log y_{1}, u_{1}, R_{1}, \log M_{1}, \log y_{1}^P, (\log P_{1,t+1}^*) \)

**PREDETERMINED VARIABLES**

**Exogenous Variables**

\(t, \log g_{1}, \log g_{1,t-1}, \log g_{1,t-2}, \log g_{1,t-3}, *_{1, t-1}, *_{1, t-2}, *_{1, t-3} \)

**Lagged Endogenous Variables**

\(\log M_{1,t-1}, \log M_{1,t-2}, \log M_{1,t-3}, \log P_{1,t-1}, \log P_{1,t-2}, \log P_{1,t-3}, \log P_{1,t-4}, \log y_{1,t-1}, \log y_{1,t-2}^P, u_{1,t-1}, u_{1,t-2}, u_{1,t-3}, R_{1,t-1}, R_{1,t-2} \)

**Expected Values Based on Prior Information**

\((\log M_{1})^*, (\log M_{1,t-1})^*, (\log M_{1,t-2})^*, (\log M_{1,t-3})^*, (\log g_{1})^*, (\log g_{1,t-1})^*, (\log g_{1,t-2})^*, (\log y_{1})^R, (\log y_{1,t-1})^R, (\log y_{1,t-2})^R, (\log y_{1,t-3})^R \)

**Foreign Variables (endoogenous in full model)**

\(\log P_{1}^R, \log y_{1}^R, \log y_{1,t-1}^R, \log y_{1,t-2}^R, \log y_{1,t-3}^R \)
Table 3
Pegged Exchange Rate Version of Nonreserve Country Submodel

EQUATIONS

(16) \( \log P_j = \beta_{j1} + T_j (\log P_j^R + \log E_j) + (1-T_j) \log N_j + \beta_{j2} t \\
+ \beta_{j3} \log y_j + \beta_{j4} R_j + \beta_{j5} \log (\Pi_{jt-1}/P_{jt-1}) + \sum_{i=0}^{3} \beta_{j,i+1} \hat{N}_j, t-1 + \epsilon_{j1} \)

(17) \( \log y_j = \alpha_{j1} + \alpha_{j2} \log y_j^{P}, t-1 + (1-\alpha_{j2}) \log y_j, t-1 + \sum_{i=0}^{3} \alpha_{j,i+1} \hat{N}_j, t-1 \\
+ \sum_{i=0}^{3} \alpha_{j,7+i} \hat{y}_j, t-1 + \sum_{i=0}^{3} \alpha_{j,11+i} \hat{R}_j, t-1 + \sum_{i=0}^{3} \alpha_{j,15+i} \hat{e}_j, t-1 + \epsilon_{j2} \)

(19) \( u_j = \gamma_{j1} + \gamma_{j2} t + \gamma_{j3} \log (y_j/y_j^{P}) + \epsilon_{j3} \)

(21) \( \frac{B_j}{H_j} = w_{j0} + w_{j1} (\log H_j - \log H_j, t-1) + w_{j2} Q_j + w_{j3} (\log M_j - \log P_j) \\
+ w_{j4} t + w_{j5} \log y_j + w_{j6} \hat{R}_j + \sum_{i=0}^{3} w_{j,7+i} \hat{N}_j, t-1 + \epsilon_{j6} \)

(24) \( \log N_j = 2 \log H_{jt-1} - \log M_{jt-2} + \eta_{j1} + \eta_{j2} (R_j - 2R_{jt-1} + R_{jt-2}) \\
+ \eta_{j3} (\log P_{jt-2} - 2 \log P_{jt-3} + \log P_{jt-4}) \\
+ \eta_{j4} (u_{jt-2} - 2u_{jt-3} - u_{jt-4}) \\
+ \eta_{j5} \{ \frac{B_j}{H_j} \hat{y}_j, t-2 - \frac{B_j}{H_j} \hat{y}_j, t-3 \} + \epsilon_{j5} \)
(25) \[ R_j = \delta_{j0} + \delta_{j1} 4[(\log P_{jt+1})^* - \log P_j] + \sum_{i=0}^{3} \delta_{j,2+i} \hat{y}_{jt-i} + \sum_{i=0}^{3} \delta_{j,6+i} \hat{E}_{jt-i} - \sum_{i=0}^{3} \delta_{j,10+i} \bar{y}_{jt-i}^R + \delta_{j,14} P_j + \delta_{j,15} 4[(\log E_{jt+1})^* - \log E_j] + \delta_{j,16} \frac{\beta_j}{H_j} + \epsilon_{j,t} \]

IDENTITIES

(18) \[ \log y_j^P = (1-\theta_j)\psi_j + \theta_j \log y_j + (1-\theta_j) \log y_j^P, t-1 \]

(20) \[ Q_j = \log P_j^R + \log E_j - \log P_j \]

(22) \[ \log H_j = \log M_j - \log u_j \]

(-) \[ (\log P_j, t+1)^* = f(\log P_j, \log P_j, t-1, \ldots) \]

(-) \[ (\log E_j, t+1)^* = f(\log E_j, \log E_j, t-1, \ldots) \]

ENDOGENOUS VARIABLES

\[ \log P_j, \log y_j, u_j, R_j, \log M_j, B_j/H_j, \log y_j^P, \log H_j, Q_j, (\log P_j, t+1)^*, (\log E_j, t+1)^* \]

PREDETERMINED VARIABLES

Exogenous Variables

\[ t, \log E_j, \log E_j, t-1, \log E_j, \log E_j, t-2, \log E_j, t-3, \log E_j, t-4 \]

\[ s_j, s_j, t-1, s_j, t-2, s_j, t-3, \log u_j \]
Lagged Endogenous Variables

\((B_j/H_j)_{t-2}, (B_j/H_j)_{t-3}, \log H_j, t-1, \log M_j, t-1, \log M_j, t-2, \log M_j, t-3, \log P_j, t-1, \log P_j, t-2, \log P_j, t-3, \log P_j, t-4, \log y_j, t-1, \log y_j, t-1^R, u_j, t-1, u_j, t-2, u_j, t-3, R_j, t-1, R_j, t-2\)

Expected Values Based on Prior Information

\((\log M_j)^*, (\log M_j, t-1)^*, (\log M_j, t-2)^*, (\log M_j, t-3)^*, (\log g_j)^*, (\log g_j, t-1)^*, (\log g_j, t-2)^*, (\log g_j, t-3)^*, (\log y_j^R)^*, (\log y_j, t-1)^*, (\log y_j^R, t-2)^*, (\log y_j^R, t-3)^*\)

Foreign Variables (endogenous in full model)

\(R_j, \log P_j^R, \log y_j^R, \log y_j, t-1, \log y_j, t-2, \log y_j, t-3\)
Table 4

Floating Exchange Rate Version of Nonreserve Country Submodel:
Changes from Pegged Exchange Rate Version

EQUATIONS

Substitute for equation (21):

$Q_j = z_{j0} + z_{j1}(\log H_j - \log H_{j,t-1}) + z_{j2}\frac{B_j}{H_j} + z_{j3}(\log H_j - \log P_j) + z_{j4}t + z_{j5}\log y_j + z_{j6}^R_j + \sum_{i=0}^{3} z_{j,7+i}^H_j + \varepsilon_{j6}'$

Add:

$\frac{B_j}{H_j} = c_{j1} + \sum_{i=0}^{3} c_{j,2+i}^2 (\log E_j,t-i - \log E_j,t-i-1) + \varepsilon_{j7}$

ENDOGENOUS VARIABLES

Add: $\log E_j$

PREDETERMINED VARIABLES

Exogenous Variables

Delete: $\log E_j, \log E_j,t-1$

Lagged Endogenous Variables

Add: $\log E_j,t-1, \log E_j,t-2, \log E_j,t-3, \log E_j,t-4$
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<thead>
<tr>
<th>Country</th>
<th>Instruments Included in List</th>
<th>Instruments Excluded Due to Multicollinearity</th>
</tr>
</thead>
<tbody>
<tr>
<td>U.S.</td>
<td>$\log H(-1), \log P(-1), \log y(-1)$, $\log y^p(-1), u(-2), u(-3), u(-4)$, $R(-1), R(-2), \hat{N}(-1), \hat{N}(-2), \hat{H}(-2), \hat{H}(-3)$, $\hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3)$</td>
<td>$\log M^<em>, \log M(-2)$, $\log P^</em>, \log P(-2)$, $\log P(-3), \log P(-4)$, $t$</td>
</tr>
<tr>
<td>U.K.</td>
<td>$\log H(-1), \log P(-1), \log \mu, \log H(-1)$, $\log y(-1), \log y^P(-1), u(-2), u(-3)$, $u(-4), R(-1), R(-2), \hat{N}(-1), \hat{N}(-2), \hat{H}(-3)$, $\hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3), B/H(-2), B/H(-3), \log E(-1)$</td>
<td>$\log M^<em>, \log M(-2)$, $\log P(-2), \log P^</em>(-2)$, $\log P(-3), \log P(-4)$, $\log E^*, t$</td>
</tr>
<tr>
<td>Canada</td>
<td>$\log M(-1), \log P(-1), \log \mu, \log y(-1), \log y^P(-1), u(-2), u(-3), u(-4)$, $R(-1), R(-2), \hat{N}(-1), \hat{N}(-2), \hat{H}(-3)$, $\hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3), B/H(-2), B/H(-3), \log E^*, \hat{E}(-3)$</td>
<td>$\log M^<em>, \log M(-2)$, $\log H(-1), \log P^</em>$, $\log P(-2), \log P(-3), \log P(-4)$, $t$</td>
</tr>
<tr>
<td>France</td>
<td>$\log M(-1), \log P(-1), \log \mu, \log H(-1)$, $\log y(-1), u(-2), u(-3), u(-4)$, $R(-1), R(-2), \hat{N}(-1), \hat{N}(-2), \hat{H}(-3)$, $\hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3), B/H(-2), B/H(-3), \log E^*$</td>
<td>$\log M^*, \log M(-2)$, $\log P(-2), \log P(-3)$, $\log P(-4), \log y^P(-1)$, $t$</td>
</tr>
<tr>
<td>Germany</td>
<td>$\log H(-1), \log P(-1), \log \mu, \log H(-1)$, $\log y(-1), \log y^P(-1), u(-2), u(-3)$, $u(-4), R(-1), R(-2), \hat{N}(-1), \hat{N}(-2), \hat{H}(-3)$, $\hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3), B/H(-2), B/H(-3), \log E(-1), \log E(-2)$</td>
<td>$\log M^*, \log M(-2)$, $\log P(-2), \log P(-3)$, $\log P(-4), t$, $\hat{E}(-6)$ [this omitted due to start date]</td>
</tr>
<tr>
<td>Italy</td>
<td>$\log M(-1), \log P(-1), \log \mu, \log y(-1), u(-2), u(-3), u(-4), R(-1), R(-2), \hat{N}(-2), \hat{N}(-3), \hat{g}, \hat{g}(-1), \hat{g}(-2), \hat{g}(-3), B/H(-2), B/H(-3), \log E^*, \hat{E}(-2), \hat{E}(-3), \hat{F}(-4)$</td>
<td>$\log M^*, \log M(-2)$, $\hat{N}(-1), \log H(-1)$, $\log P(-2), \log P(-3)$, $\log P(-4), \log y^P(-1)$, $t$, $\hat{E}(-5)$ [this omitted due to start date]</td>
</tr>
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<td>Country</td>
<td>Variables</td>
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</tr>
<tr>
<td>-------------</td>
<td>---------------------------------------------------------------------------</td>
<td></td>
</tr>
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<td>log M(-1), log P(-1), log μ, log γ(-1), log γ*, log H(-2), log H(-1),</td>
<td></td>
</tr>
<tr>
<td></td>
<td>u(-2), u(-3), u(-4), R(-1), R(-2),</td>
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<td></td>
<td>H(-1), H(-2), H(-3),  ̂g,  ̂g(-1),  ̂g(-2),</td>
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<td>̂g(-3), B/H(-2), B/H(-3),  ̂p(-3),</td>
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</tr>
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<td></td>
<td>log E(-1),  ̂E(-4)</td>
<td></td>
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<td></td>
<td>log γ(-1), log γ*(-1), u(-2), u(-3),</td>
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<tr>
<td></td>
<td>u(-4), R(-1), R(-2), H(-1), H(-2), H(-3),</td>
<td></td>
</tr>
<tr>
<td></td>
<td>̂g,  ̂g(-1),  ̂g(-2),  ̂g(-3), B/H(-2),</td>
<td></td>
</tr>
<tr>
<td></td>
<td>B/H(-3), log E*,  ̂E(-1),  ̂E(-3)</td>
<td></td>
</tr>
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</table>

[The last two omitted due to start date]
Table 6

Money Stock Definitions for the NBER International Transmission Model

<table>
<thead>
<tr>
<th>Country</th>
<th>Money Concept</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Canada</td>
<td>$M_1$</td>
<td>Slightly preferable to $M_2$ for $y$ and $P$ equations, but not reaction functions.</td>
</tr>
<tr>
<td>France</td>
<td>$M_2$</td>
<td>Tied for $y$ and $P$ equations, but better reaction function.</td>
</tr>
<tr>
<td>Germany</td>
<td>$M_2$</td>
<td>Slightly preferable for $y$ and $P$ equations, preferable for reaction functions.</td>
</tr>
<tr>
<td>Italy</td>
<td>$M_1$</td>
<td>Preferable for $y$ equations and reaction functions.</td>
</tr>
<tr>
<td>Japan</td>
<td>$M_1$</td>
<td>Preferable for $y$ equations and reaction functions.</td>
</tr>
<tr>
<td>Netherlands</td>
<td>$M_2$</td>
<td>Slightly preferable for $y$ and $P$ equations, preferable for reaction functions.</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>$M_1$</td>
<td>Tied for $y$ and $P$ equations, slightly preferred for reaction functions.</td>
</tr>
<tr>
<td>United States</td>
<td>$M_1$</td>
<td>Preferable for $y$ equations and reaction functions.</td>
</tr>
<tr>
<td>-----------</td>
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<tr>
<td>United States</td>
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</table>

**Note:** The data represents the approximate exchange rates for selected countries based on the indicated years. The rates are expressed in terms of the currency of the country listed. The values are approximate due to the nature of historical currency fluctuations.
<table>
<thead>
<tr>
<th>Country</th>
<th>Foreign Exchange (1)</th>
<th>Foreign Credit (2)</th>
<th>Foreign Trade (3)</th>
<th>Foreign Deposits (4)</th>
<th>Foreign Borrower (5)</th>
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</thead>
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<td>2.0%</td>
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<tr>
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<tr>
<td>Mexico</td>
<td>2.6%</td>
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<td>Brazil</td>
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<td>India</td>
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<td>4.2%</td>
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<td>6.5%</td>
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</tbody>
</table>

**Notes:**
1. Foreign Exchange includes short-term and long-term foreign exchange operations.
2. Foreign Credit includes foreign loans and credits.
3. Foreign Trade includes exports and imports.
4. Foreign Deposits includes deposits held by foreigners in domestic banks.
5. Foreign Borrower includes foreign borrowing from domestic banks.

**Revised Price Equations (2) (and 16) with T = 0**

**Table 7A**
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**Note:** The data represents annual growth rates in real per capita GDP. The data is sourced from various economic reports and is subject to revision.
<table>
<thead>
<tr>
<th>Country</th>
<th>X1</th>
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<td>50°</td>
<td>105°</td>
<td>9°</td>
</tr>
<tr>
<td>Germany</td>
<td>49°</td>
<td>106°</td>
<td>9°</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>52°</td>
<td>107°</td>
<td>9°</td>
</tr>
<tr>
<td>United States</td>
<td>55°</td>
<td>108°</td>
<td>9°</td>
</tr>
</tbody>
</table>

*Table 6*

Volume Equation and H.R.E. (19)
<table>
<thead>
<tr>
<th>Country</th>
<th>Exchange Rate</th>
<th>Real Income Growth</th>
</tr>
</thead>
<tbody>
<tr>
<td>Japan</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>Italy</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>France</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>Canada</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>Netherlands</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>Germany</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>9000</td>
<td>-</td>
</tr>
<tr>
<td>Sweden</td>
<td>9000</td>
<td>-</td>
</tr>
</tbody>
</table>

**Note:** The table presents exchange rates and real income growth for various countries. The real income growth values are represented as negative (-) indicating a decrease. The exchange rates are shown in a specific format, possibly indicating currency values. The table is part of a larger document, possibly discussing economic principles or data analysis.
**TABLE 10**

MONEY SUPPLY REACTION FUNCTIONS (12) AND (24)

<table>
<thead>
<tr>
<th>Country</th>
<th>Const. $\eta_{11}$</th>
<th>$\Delta^2 R_j/\eta_{12}$</th>
<th>$\Delta^2 F_{jt-2}/\eta_{13}$</th>
<th>$\Delta^2 u_{jt-2}/\eta_{14}$</th>
<th>$\Delta(B_{jt}/H_{jt})<em>{t-2}/\eta</em>{15}$</th>
<th>$r^2$</th>
<th>S.E.E.</th>
<th>D-W</th>
</tr>
</thead>
<tbody>
<tr>
<td>United States</td>
<td>.000126 (.197)</td>
<td>.003 (2.57)</td>
<td>-.0246 (-1.56)</td>
<td>.289 (-1.57)</td>
<td>---</td>
<td>.99953</td>
<td>.00568</td>
<td>2.14</td>
</tr>
<tr>
<td>United Kingdom</td>
<td>.000464 (.275)</td>
<td>-.797 (-3.41)</td>
<td>-.0948 (-.752)</td>
<td>-3.30 (-2.17)</td>
<td>.0202 (-.574)</td>
<td>.99528</td>
<td>.0220</td>
<td>2.81</td>
</tr>
<tr>
<td>Germany</td>
<td>-.00047 (.21)</td>
<td>-.123 (-0.63)</td>
<td>.0016 (.005)</td>
<td>-.414 (-.78)</td>
<td>.036 (-1.38)</td>
<td>.99859</td>
<td>.0202</td>
<td>3.08</td>
</tr>
<tr>
<td>Netherlands</td>
<td>.00102 (.445)</td>
<td>.374 (1.68)</td>
<td>-.095 (-.65)</td>
<td>.266 (.15)</td>
<td>.0123 (.34)</td>
<td>.99876</td>
<td>.0206</td>
<td>2.98</td>
</tr>
<tr>
<td>Canada</td>
<td>.00046 (.204)</td>
<td>-.3856 (-1.17)</td>
<td>-.086 (-.935)</td>
<td>-.0019 (-.321)</td>
<td>-1.104 (-2.24)</td>
<td>.99757</td>
<td>.020</td>
<td>2.51</td>
</tr>
<tr>
<td>France</td>
<td>.00049 (0.31)</td>
<td>-.421 (-2.37)</td>
<td>-.414 (-2.25)</td>
<td>-1.82 (-1.06)</td>
<td>.110 (2.26)</td>
<td>.99949</td>
<td>.0143</td>
<td>2.54</td>
</tr>
<tr>
<td>Italy</td>
<td>.00017 (.07)</td>
<td>.129 (.23)</td>
<td>.152 (.77)</td>
<td>-.517 (-1.21)</td>
<td>.167 (1.77)</td>
<td>.99933</td>
<td>.0214</td>
<td>3.04</td>
</tr>
<tr>
<td>Japan</td>
<td>.000015 (.007)</td>
<td>-.4.420 (-1.74)</td>
<td>-.138 (-.904)</td>
<td>-2.516 (-1.34)</td>
<td>-1.065 (-1.31)</td>
<td>.99958</td>
<td>.0200</td>
<td>2.62</td>
</tr>
</tbody>
</table>

1957 I - 1976 IV and 1*MK2206 for FR, GE, and ME.

Money Definitions: See Table 6.

t-values in parentheses.
<table>
<thead>
<tr>
<th>Country</th>
<th>Exchange Rate</th>
<th>Interest Rate</th>
<th>GDP Growth</th>
</tr>
</thead>
<tbody>
<tr>
<td>Japan</td>
<td>120.00 896.00</td>
<td>55.1%</td>
<td>2.3%</td>
</tr>
<tr>
<td>Italy</td>
<td>1120.00 512.00</td>
<td>100.0%</td>
<td>-0.8%</td>
</tr>
<tr>
<td>France</td>
<td>701.00 499.00</td>
<td>85.1%</td>
<td>1.7%</td>
</tr>
<tr>
<td>Canada</td>
<td>621.00 599.00</td>
<td>90.0%</td>
<td>2.1%</td>
</tr>
<tr>
<td>Mexico</td>
<td>512.00 490.00</td>
<td>100.0%</td>
<td>-0.4%</td>
</tr>
<tr>
<td>Germany</td>
<td>692.00 599.00</td>
<td>75.1%</td>
<td>0.6%</td>
</tr>
<tr>
<td>Brazil</td>
<td>194.00 117.00</td>
<td>100.0%</td>
<td>2.5%</td>
</tr>
</tbody>
</table>

(11) Interest Rate Equations (2) and (3)